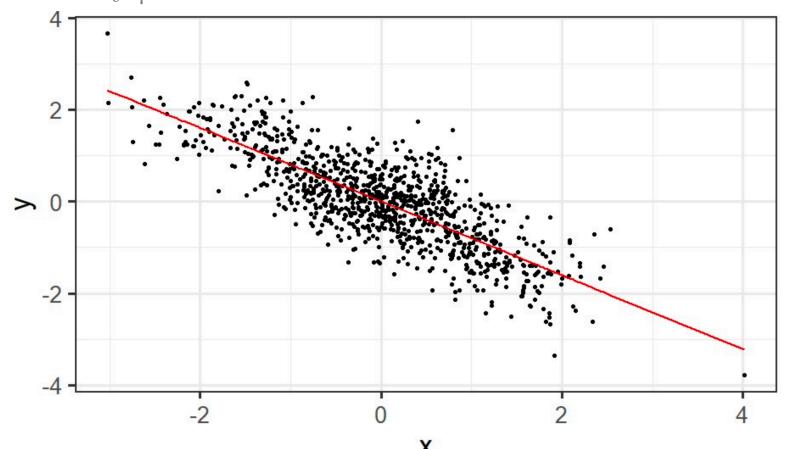
Model Agnostic Interpretability

Making sense of complex models

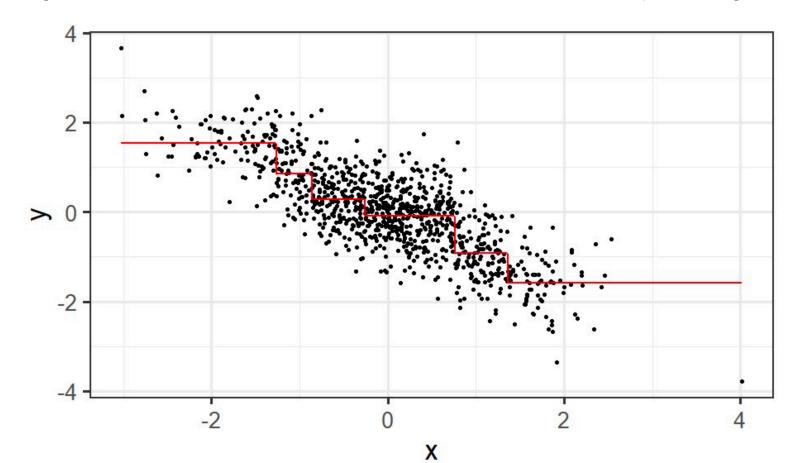
Interpretable Models

Generalized Linear Models: If x increases by 1 unit, y increases by β units



Interpretable Models

<u>Decision Trees</u>: If conditions A, B, and C are satisfied, then then y is If conditions !A and D are satisfied, then y is....



Other Models

Random Forests?

No.

Gradient Boosting Machines?

Sorry, no.

Neural Networks?

Try again.

Support Vector Machines?

Nah.

Naive Bayes?



Motivation

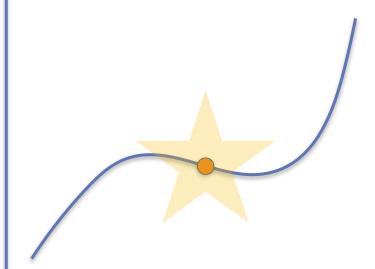
- Humans want to interpret and understand model behavior
- We have questions!
 - Why was this person's loan application rejected?
 - Why is the symptom occurring in this patient?
 - Why is the stock price expected to go down?
- Interpretations can be model and context dependent
 - <u>Model dependent</u>: variable importance in regression has different implications than variable importance in trees.
 - <u>Context dependent</u>: the effect of, say age, on a response may depend on an individual's age and other factors. (i.e. nonlinearity)

Why so important?

- Fairness/Transparency
 - Understanding modeled decisions improves consumer trust
 - Interpretations reveal model behavior on different groups of people (including marginalized groups)
- Model Robustness and Integrity
 - Interpretability methods can reveal odd model behavior or issues with overfitting.
- Adverse Action notice requirements
 - Equal Credit Opportunity Act (ECOA)
 - Fair Credit Reporting Act (FCRA)
 - More likely to come with the tide of Ethical Machine Learning.

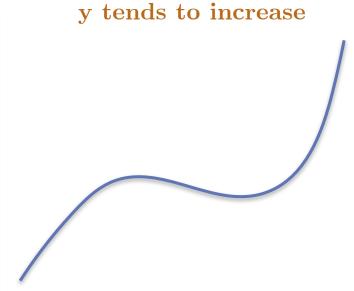
Local

When x=10, y decreases as x increases



Global

As x increases, y tends to increase



	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
Model Agnostic	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
$egin{aligned} \mathbf{Model} \\ \mathbf{Agnostic} \end{aligned}$	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

Boston Dataset

```
#' crim -- per capita crime rate by town.
#' zn -- proportion of residential land zoned for lots over 25,000 sq.ft.
#' indus -- proportion of non-retail business acres per town.
#' chas -- Charles River dummy variable (= 1 if tract bounds river; 0
otherwise). nox nitrogen oxides concentration (parts per 10 million).
#' rm -- average number of rooms per dwelling.
#' age -- proportion of owner-occupied units built prior to 1940.
#' dis -- weighted mean of distances to five Boston employment centres.
#rad -index of accessibility to radial highways.
#' tax -- full-value property-tax rate per \$10,000.
#' ptratio -- pupil-teacher ratio by town.
#' black -- 1000(Bk - 0.63)2 where Bk is the proportion of black residents
by town.
#' lstat lower status of the population (percent).
#' medv -- median value of owner-occupied homes in \$1000s.
```

Predicting target nox - nitrogen oxides concentration (parts per 10 million).

	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
$egin{aligned} \mathbf{Model} \\ \mathbf{Agnostic} \end{aligned}$	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

Permutation Importance

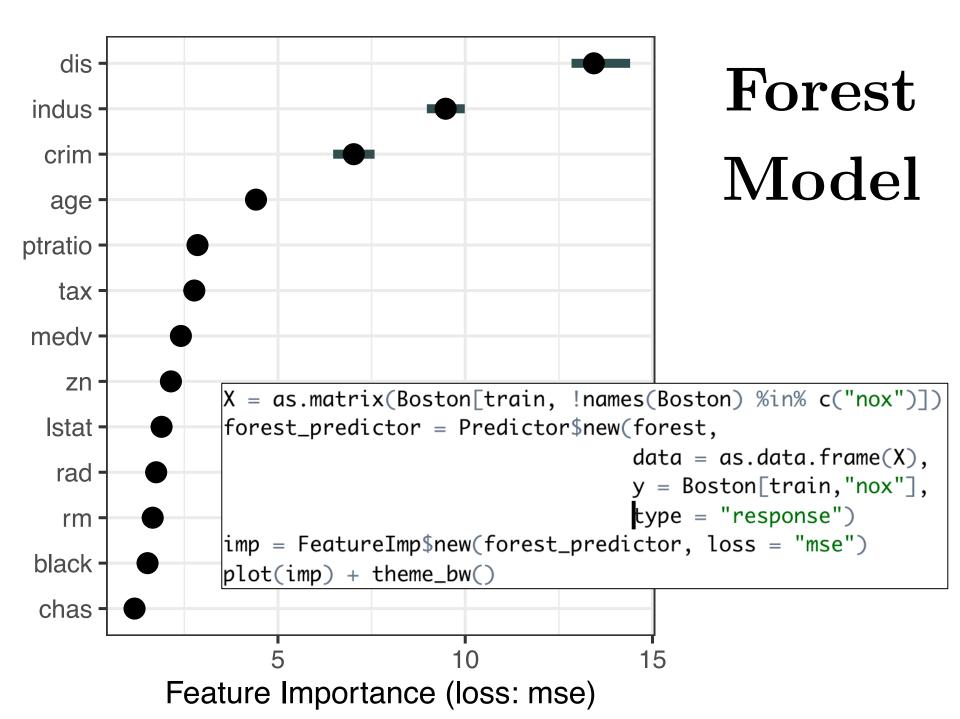
"Let me show you how much worse the predictions of our model get if we input randomly shuffled data values for each variable"

Permutation Importance

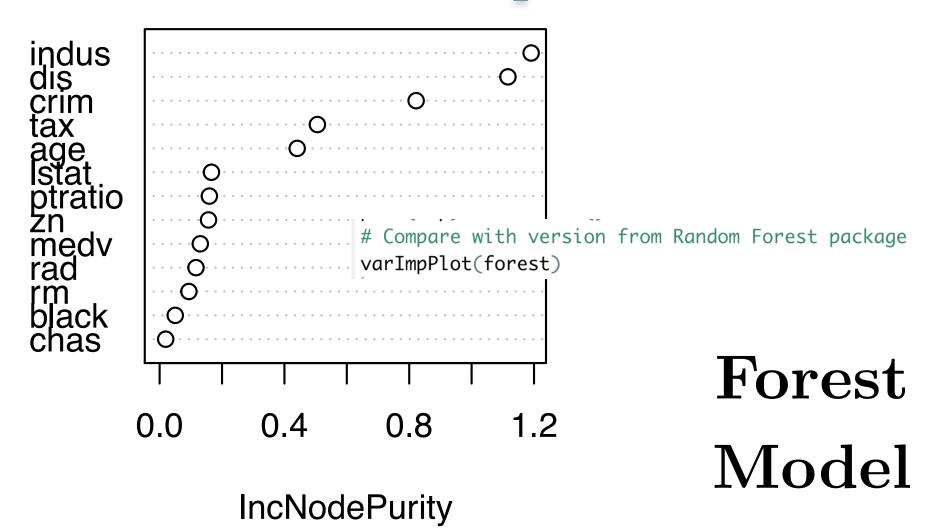
- If a variable is important, the model should get worse when that variable is removed.
- To make a direct comparison, rather than remove the variable from the model, we'll destroy its signal.
- By randomly permuting that values in that column of data, we *break* the true relationship and make it nonsense.
- How much worse does the model get when we do? (on average, over default n=5 permutations)
 - => Permutation Feature Importance

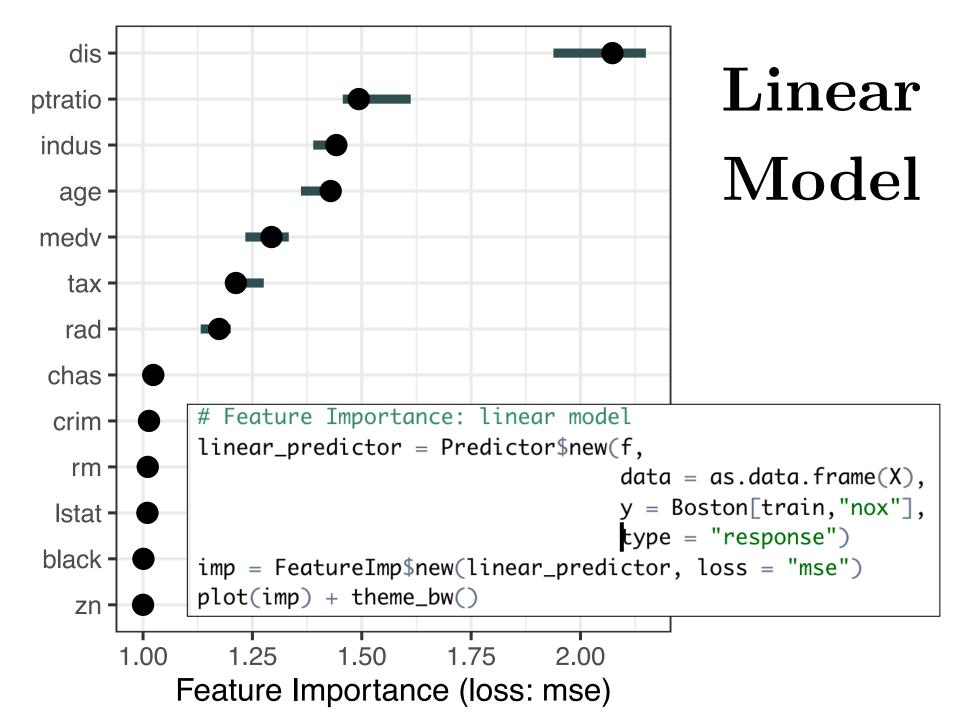
```
train = sample(c(T,F),nrow(Boston),replace=T,p=c(0.75,0.25))
forest = randomForest(nox~.,data=Boston[train,])
```

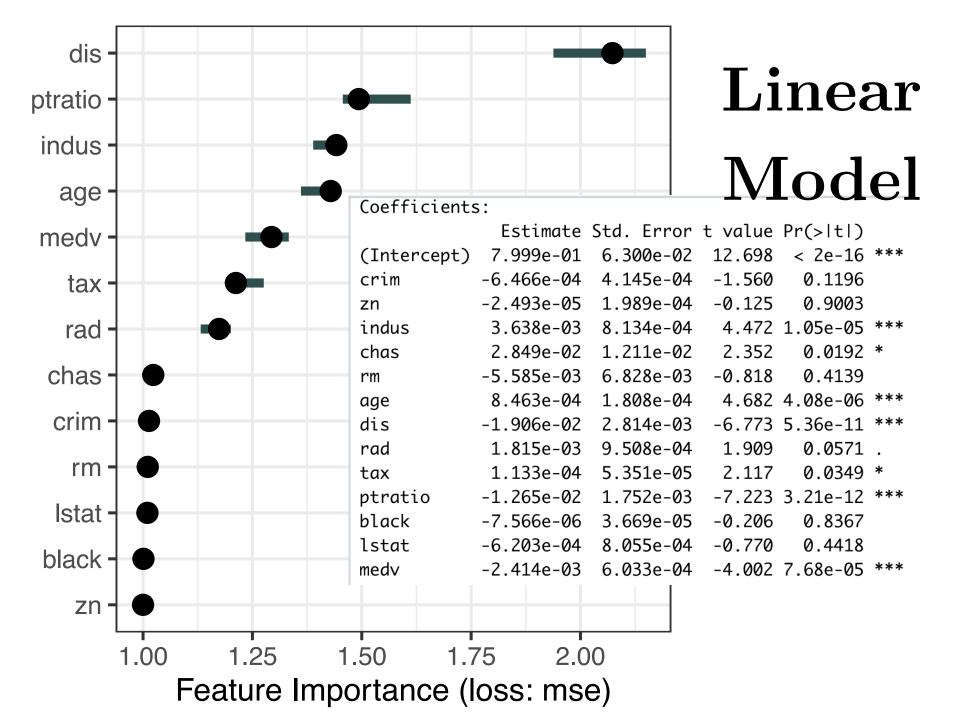
```
# Linear Model for Comparison
f = lm(nox~., data=Boston[train,])
```



Compare to randomForest Variable Importance







	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
Model Agnostic	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

"Let me show you how the predictions for each observation change if we vary the feature of interest."

- This is a *local* method because it visualizes the dependence of an *individual prediction* on a given input variable.
- Fix all other variables for a single observation while varying the feature of interest.
- Plot the resulting prediction vs the feature of interest.

dis	ptratio	medv	indus	age	ax	rad	Actual Y	$egin{array}{c} \operatorname{Pred} \ Y \end{array}$
3	12.1	13	22.6	90	234	4.3	0.469	0.454
5	17.2	41	9.1	71	326	2.5	0.538	0.512
6	20.1	31	15.2	88	222	5.1	0.458	0.470
2	15	22	5.2	45	430	6.3	0.556	0.561

Choose a variable of interest and a single observation.

dis	ptratio	medv	indus	age	ax	rad	Actual V	$egin{array}{c} \mathbf{Pred} \ \mathbf{V} \end{array}$
3	12.1	13	22.6	90	234	4.3	0.469	0.454
5	17.2	41	9.1	71	326	2.5	0.538	0.512
6	20.1	31	15.2	88	222	5.1	0.458	0.470
2	15	22	5.2	45	430	6.3	0.556	0.561

Choose a variable of interest and a single observation.

dis	ptratio	medv	indus	age	tax	rad	Actual Y	$egin{array}{c} \mathbf{Pred} \ \mathbf{Y} \end{array}$
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	

Replicate single observation, holding constant data values on other variables.

${ m dis}$	ptratio	medv	indus	age	ax	rad	Actual Y	$egin{array}{c} \mathbf{Pred} \ \mathbf{Y} \end{array}$
3	12.1	13	22.6	90	200	4.3	0.469	
3	12.1	13	22.6	90	201	4.3	0.469	
3	12.1	13	22.6	90	202	4.3	0.469	
3	12.1	13	22.6	90	203	4.3	0.469	
3	12.1	13	22.6	90	204	4.3	0.469	
3	12.1	13	22.6	90	205	4.3	0.469	
3	12.1	13	22.6	90	206	4.3	0.469	

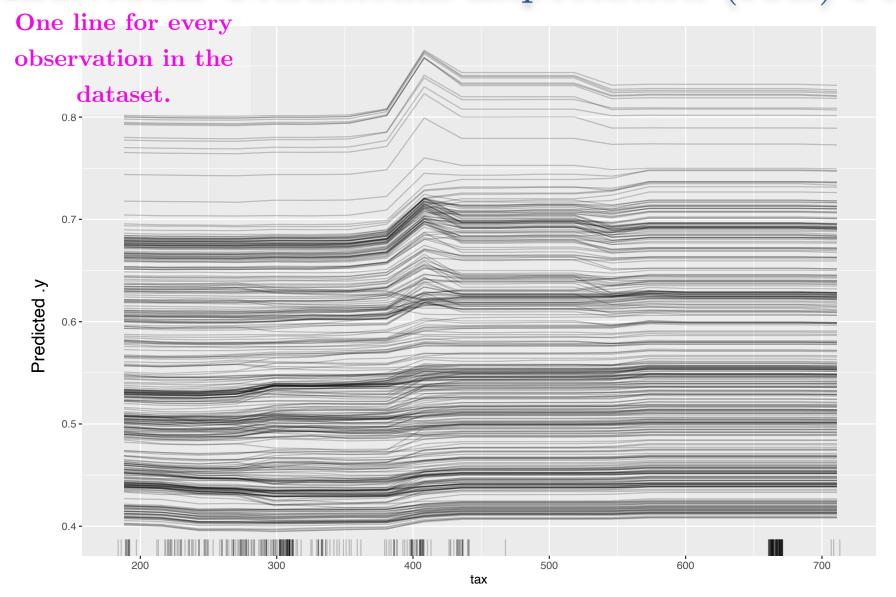
Fill in values for variable of interest across the entire range of the variable

dis	ptratio	medv	indus	age	tax	rad	Actual Y	$egin{array}{c} \mathbf{Pred} \ \mathbf{Y} \end{array}$
3	12.1	13	22.6	90	200	4.3	0.469	0.448
3	12.1	13	22.6	90	201	4.3	0.469	0.449
3	12.1	13	22.6	90	202	4.3	0.469	0.450
3	12.1	13	22.6	90	203	4.3	0.469	0.450
3	12.1	13	22.6	90	204	4.3	0.469	0.451
3	12.1	13	22.6	90	205	4.3	0.469	0.452
3	12.1	13	22.6	90	206	4.3	0.469	0.452

Use the model to generate predictions for this simulated data.

Typically repeat for each observation (or large sample)

```
#' Individual Conditional Expectation (ICE) Plots
#'
set.seed(13)
pdps = FeatureEffects$new(forest_predictor, method='ice')
pdps$plot() #All charts
pdps$plot(c("tax")) #Subset of Charts
```



An ICE plot displays the relationship between the prediction and a feature for *each* observation separately, resulting in one line per observation

Individual Conditional Expectation (ICE) Plot 0.8 0.7 -Predicted .y 0.6 -0.5 -

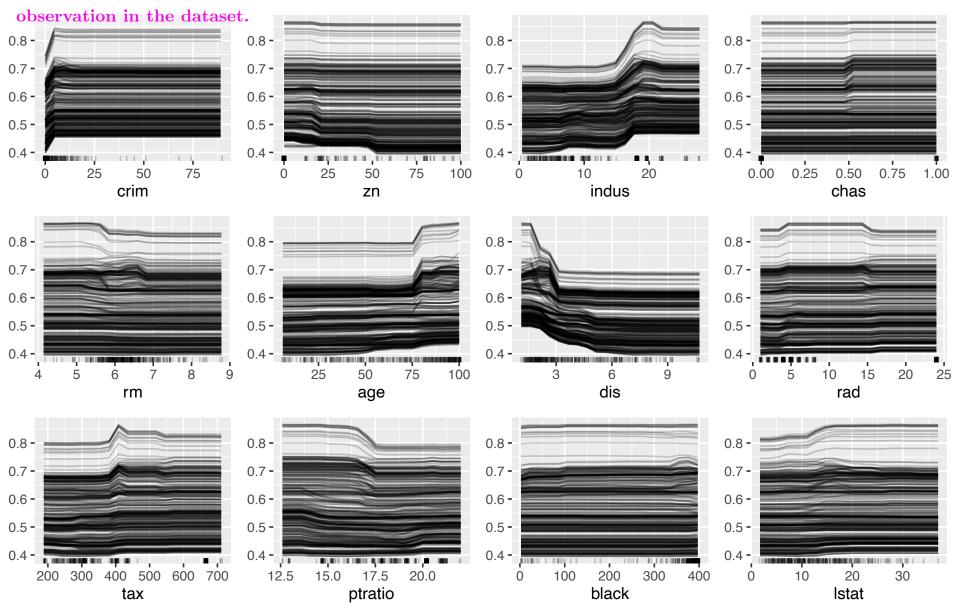
An ICE plot displays the relationship between the prediction and a feature for *each* observation separately, resulting in one line per observation

0.4 -

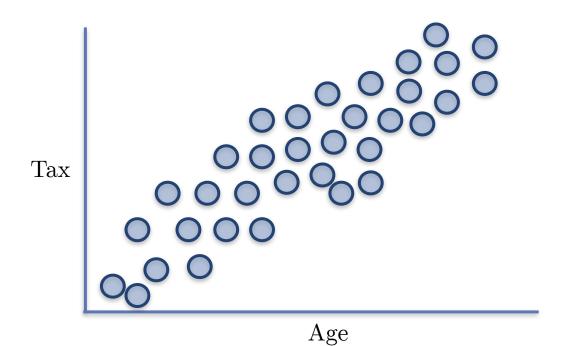
Ticks on horizontal axis show

distribution of variable of interest ('dis')

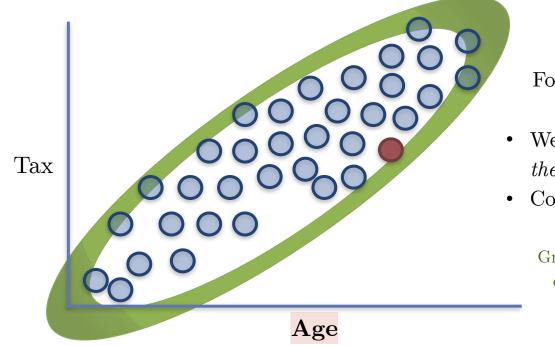
One line for every



If variable of interest is correlated with other inputs, some of the simulated data may be invalid!



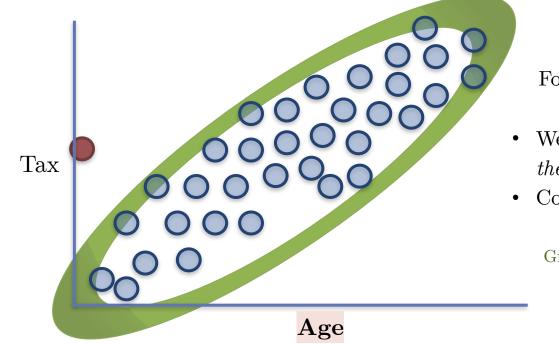
If variable of interest is correlated with other inputs, some of the simulated data may be invalid!



For this red point of interest, and for the variable of interest **Age:**

- We'll keep everything the same, and vary the age across some replicates.
- Computes F(y|x) for each replicate x

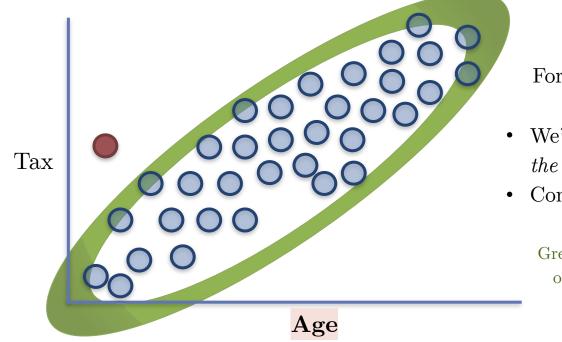
If variable of interest is correlated with other inputs, some of the simulated data may be invalid!



For this red point of interest, and for the variable of interest **Age:**

- We'll keep everything the same, and vary the age across some replicates.
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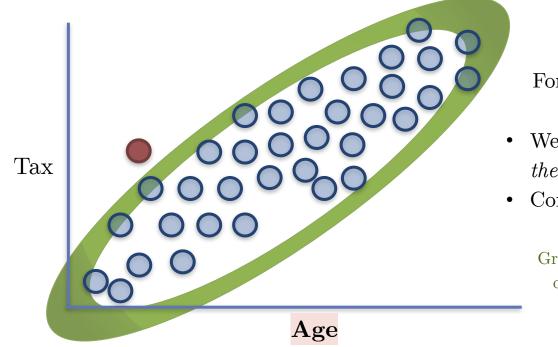
If variable of interest is correlated with other inputs, some of the simulated data may be invalid!



For this red point of interest, and for the variable of interest **Age:**

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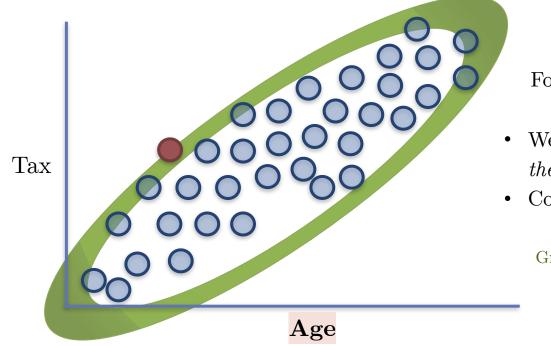
If variable of interest is correlated with other inputs, some of the simulated data may be invalid!



For this red point of interest, and for the variable of interest **Age:**

- We'll keep everything the same, and vary the age across some replicates.
- Computes F(y|x) for each replicate x

If variable of interest is correlated with other inputs, some of the simulated data may be invalid!

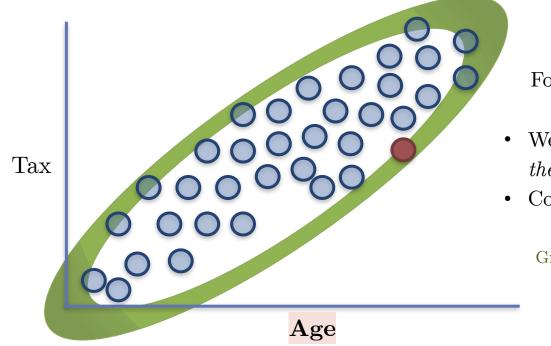


For this red point of interest, and for the variable of interest **Age:**

- We'll keep everything the same, and vary the age across some replicates.
- Computes $F(y|\mathbf{x})$ for each replicate \mathbf{x}

ICE: Problems with Multicollinearity

If variable of interest is correlated with other inputs, some of the simulated data may be invalid!



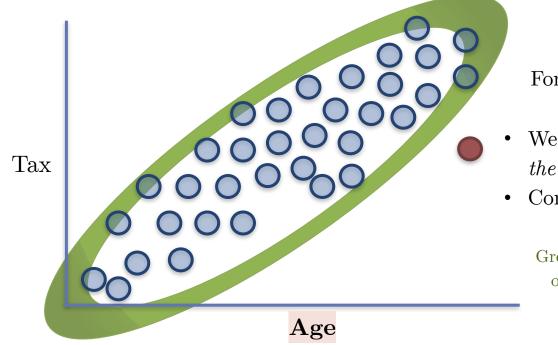
For this red point of interest, and for the variable of interest **Age:**

- We'll keep everything the same, and vary the age across some replicates.
- Computes F(y|x) for each replicate x

Green Ellipse shows what is *likely* to occur based on the *bivariate* distribution of Age and Tax.

ICE: Problems with Multicollinearity

If variable of interest is correlated with other inputs, some of the simulated data may be invalid!



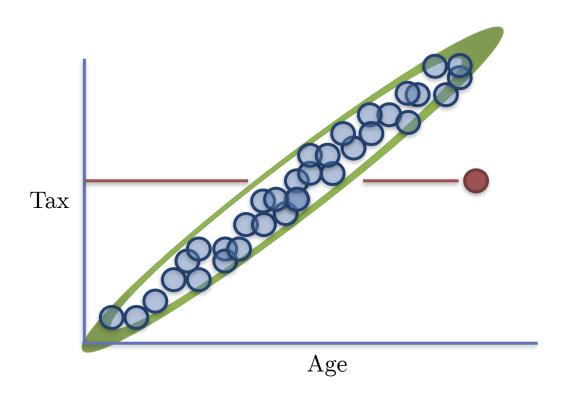
For this red point of interest, and for the variable of interest **Age:**

- We'll keep everything the same, and vary the age across some replicates.
- Computes $F(y|\mathbf{x})$ for each replicate \mathbf{x}

Green Ellipse shows what is *likely* to occur based on the *bivariate* distribution of Age and Tax.

ICE: Problems with Multicollinearity

More Severe Correlation => More Severe Problems.



Summary: Individual Conditional Expectation (ICE)

Advantages

- Intuitive to understand. One line represents to predictions for one observation if we vary the feature of interest.
- Capable of uncovering *heterogeneous* relationships (when the feature of interest has different impact for different observations)

Summary: Individual Conditional Expectation (ICE)

Disadvantages

- Difficult to process (computationally and visually) with too many observations, but sampling may lose interesting signal.
- If variable of interest is correlated with other inputs, some of the simulated data may be invalid!
- Can sometimes reveal interesting interactions, but requires a *lot* of exploration.
- Can only meaningfully display relationship of one variable

Types of Model Interpretability

	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
$egin{array}{c} \mathbf{Model} \\ \mathbf{Agnostic} \end{array}$	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

Partial Dependence

"Let me show you what the model predicts on average when each observation has the value v for that feature. We'll ignore whether the value v makes sense for all data instances."

Attempts to show the <u>marginal</u> effect of inputs on the target.

Marginal: relating to a random variable that is obtained from a function of several random variables by averaging over all possible values of the other variables

In other words, what is the *expectation* (mean/average) of our predictive model $f(\mathbf{x})$ across values of a single variable x_i ?

In OTHER words, what if we average all those lines on the ICE plot?

${f dis}$	ptratio	medv	indus	age	ax	rad	Actual	Pred_{-}
				J			\mathbf{Y}	\mathbf{Y}
3	12.1	13	22.6	90	234	4.3	0.469	0.454
5	17.2	41	9.1	71	326	2.5	0.538	0.512
6	20.1	31	15.2	88	222	5.1	0.458	0.470
2	15	22	5.2	45	430	6.3	0.556	0.561

Choose a variable of interest.

dis	ptratio	$\operatorname{med}\mathbf{v}$	indus	age	tax	$_{ m rad}$	Actual Y	$egin{array}{c} \operatorname{Pred} \ Y \end{array}$	dis	ptratio	$\operatorname{med}\mathbf{v}$	indus	age	tax	rad	Actual Y	$egin{array}{c} ext{Pred} \ ext{Y} \end{array}$
3	12.1	13	22.6	90		4.3	0.469		3	12.1	13	22.6	90	2	4.3	0.469	
5	17.2	41	9.1	71		2.5	0.538		5	17.2	41	9.1	71		2.5	0.538	
6	20.1	31	15.2	88		5.1	0.458		6	20.1	31	15.2	88		5.1	0.458	
2	15	22	5.2	45		6.3	0.556		2	15	22	5.2	45		6.3	0.556	
				4											-		
dis	ptratio	$\operatorname{med} \mathbf{v}$	indus	age	tax	$_{ m rad}$	Actual Y	Pred Y	dis	ptratio	medv	indus	age	tax	rad	Actual Y	$rac{ ext{Pred}}{ ext{Y}}$
3	12.1	13	22.6	90		4.3	0.469		3	12.1	13	22.6	90	1	4.3	0.469	
5	17.2	41	9.1	71		2.5	0.538		5	17.2	41	9.1	71		2.5	0.538	
6	20.1	31	15.2	88		5.1	0.458		6	20.1	31	15.2	88	1	5.1	0.458	
2	15	22	5.2	45		6.3	0.556		2	15	22	5.2	45		6.3	0.556	
				3										And an age of the same	*		
dis	ptratio	medv	indus	age	tax	$_{ m rad}$	Actual Y	$rac{ ext{Pred}}{ ext{Y}}$	dis	ptratio	$_{ m medv}$	indus	age	tax	rad	Actual Y	Pred Y
3	12.1	13	22.6	90		4.3	0.469		3	12.1	13	22.6	90		4.3	0.469	
5	17.2	41	9.1	71		2.5	0.538		5	17.2	41	9.1	71		2.5	0.538	
6	20.1	31	15.2	88	9	5.1	0.458		6	20.1	31	15.2	88		5.1	0.458	
2	15	22	5.2	45		6.3	0.556		2	15	22	5.2	45		6.3	0.556	
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dis	ptratio	$_{ m medv}$	indus	age	tax	$_{ m rad}$	Actual Y	$egin{array}{c} \operatorname{Pred} & & & & & & & & & & & & & & & & & & &$	dis	ptratio	$_{ m medv}$	indus	age	tax	$_{ m rad}$	Actual Y	$egin{array}{c} \operatorname{Pred} \ \mathbf{Y} \end{array}$
3	12.1	13	22.6	90		4.3	0.469		3	12.1	13	22.6	90	1	4.3	0.469	
5	17.2	41	9.1	71		2.5	0.538		5	17.2	41	9.1	71		2.5	0.538	
6	20.1	31	15.2	88	9	5.1	0.458		6	20.1	31	15.2	88		5.1	0.458	
2	15	22	5.2	45		6.3	0.556		2	15	22	5.2	45		6.3	0.556	

Replicate your *dataset*, holding constant all values except the variable of interest.

dis	ptratio	$\operatorname{med}\mathbf{v}$	indus	age	tax	rad	Actual Y	$egin{array}{c} \operatorname{Pred} \ Y \end{array}$	dis	ptratio	$_{ m medv}$	indus	age	tax	$_{ m rad}$	Actual Y	Pred Y
3	12.1	13	22.6	90	200	4.3	0.469		3	12.1	13	22.6	90	204	4.3	0.469	
5	17.2	41	9.1	71	200	2.5	0.538		5	17.2	41	9.1	71	204	2.5	0.538	
6	20.1	31	15.2	88	200	5.1	0.458		6	20.1	31	15.2	88	204	5.1	0.458	
2	15	22	5.2	45	200	6.3	0.556		2	15	22	5.2	45	204	6.3	0.556	
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dis	ptratio	$\operatorname{med} \mathbf{v}$	indus	age	tax	$_{ m rad}$	Actual Y	$egin{array}{c} \operatorname{Pred} \ Y \end{array}$	dis	ptratio	medv	indus	age	tax	rad	Actual Y	$rac{ ext{Pred}}{ ext{Y}}$
3	12.1	13	22.6	90	201	4.3	0.469		3	12.1	13	22.6	90	205	4.3	0.469	
5	17.2	41	9.1	71	201	2.5	0.538		5	17.2	41	9.1	71	205	2.5	0.538	
6	20.1	31	15.2	88	201	5.1	0.458		6	20.1	31	15.2	88	205	5.1	0.458	
2	15	22	5.2	45	201	6.3	0.556		2	15	22	5.2	45	205	6.3	0.556	
				2											w -		
dis	ptratio	$\mathrm{med}\mathbf{v}$	indus	age	tax	$_{ m rad}$	Actual Y	$egin{array}{c} \operatorname{Pred} \ Y \end{array}$	dis	ptratio	$_{ m medv}$	indus	age	tax	rad	Actual Y	Pred Y
3	12.1	13	22.6	90	202	4.3	0.469		3	12.1	13	22.6	90	206	4.3	0.469	
5	17.2	41	9.1	71	202	2.5	0.538		5	17.2	41	9.1	71	206	2.5	0.538	
6	20.1	31	15.2	88	202	5.1	0.458		6	20.1	31	15.2	88	206	5.1	0.458	
2	15	22	5.2	45	202	6.3	0.556		2	15	22	5.2	45	206	6.3	0.556	
				5											*		
dis	ptratio	$\operatorname{med}\mathbf{v}$	indus	age	tax	rad	Actual Y	$egin{array}{c} \operatorname{Pred} & & & & & & & & & & & & & & & & & & &$	dis	ptratio	$\operatorname{med}\mathbf{v}$	indus	age	tax	rad	Actual Y	$egin{array}{c} \operatorname{Pred} \ \mathbf{Y} \end{array}$
3	12.1	13	22.6	90	203	4.3	0.469		3	12.1	13	22.6	90	207	4.3	0.469	
5	17.2	41	9.1	71	203	2.5	0.538		5	17.2	41	9.1	71	207	2.5	0.538	
6	20.1	31	15.2	88	203	5.1	0.458		6	20.1	31	15.2	88	207	5.1	0.458	
2	15	22	5.2	45	203	6.3	0.556		2	15	22	5.2	45	207	6.3	0.556	

Fill in values for variable of interest for each replicated dataset across the range of the variable.

dis	ptratio	medv	indus	age	tax	rad	Actual Y	Pred Y	dis	ptratio	medv	indus	age	tax	$_{ m rad}$	Actual Y	Pred Y
3	12.1	13	22.6	90	200	4.3	0.469	0.426	3	12.1	13	22.6	90	204	4.3	0.469	0.510
5	17.2	41	9.1	71	200	2.5	0.538	0.532	5	17.2	41	9.1	71	204	2.5	0.538	0.532
6	20.1	31	15.2	88	200	5.1	0.458	0.445	6	20.1	31	15.2	88	204	5.1	0.458	0.495
2	15	22	5.2	45	200	6.3	0.556	0.550	2	15	22	5.2	45	204	6.3	0.556	0.532
							9		•								
dis	ptratio	medv	indus	age	tax	rad	Actual Y	Pred Y	dis	ptratio	medv	indus	age	tax	$_{ m rad}$	Actual Y	Pred Y
3	12.1	13	22.6	90	201	4.3	0.469	0.436	3	12.1	13	22.6	90	205	4.3	0.469	0.426
5	17.2	41	9.1	71	201	2.5	0.538	0.542	5	17.2	41	9.1	71	205	2.5	0.538	0.532
6	20.1	31	15.2	88	201	5.1	0.458	0.445	6	20.1	31	15.2	88	205	5.1	0.458	0.485
2	15	22	5.2	45	201	6.3	0.556	0.523	2	15	22	5.2	45	205	6.3	0.556	0.561
							9									3	
dis	ptratio	medv	indus	age	tax	rad	Actual Y	Pred Y	dis	ptratio	medv	indus	age	tax	rad	Actual Y	Pred Y
3	12.1	13	22.6	90	202	4.3	0.469	0.526	3	12.1	13	22.6	90	206	4.3	0.469	0.469
5	17.2	41	9.1	71	202	2.5	0.538	0.532	5	17.2	41	9.1	71	206	2.5	0.538	0.532
6	20.1	31	15.2	88	202	5.1	0.458	0.475	6	20.1	31	15.2	88	206	5.1	0.458	0.495
2	15	22	5.2	45	202	6.3	0.556	0.561	2	15	22	5.2	45	206	6.3	0.556	0.532
							9									2	
dis	ptratio	$\operatorname{med} v$	indus	age	tax	rad	Actual Y	Pred Y	${ m dis}$	ptratio	$_{ m medv}$	indus	age	tax	rad	Actual Y	Pred Y
3	12.1	13	22.6	90	203	4.3	0.469	0.426	3	12.1	13	22.6	90	207	4.3	0.469	0.426
5	17.2	41	9.1	71	203	2.5	0.538	0.532	5	17.2	41	9.1	71	207	2.5	0.538	0.532
6	20.1	31	15.2	88	203	5.1	0.458	0.445	6	20.1	31	15.2	88	207	5.1	0.458	0.445
2	15	22	5.2	45	203	6.3	0.556	0.550	2	15	22	5.2	45	207	6.3	0.556	0.550

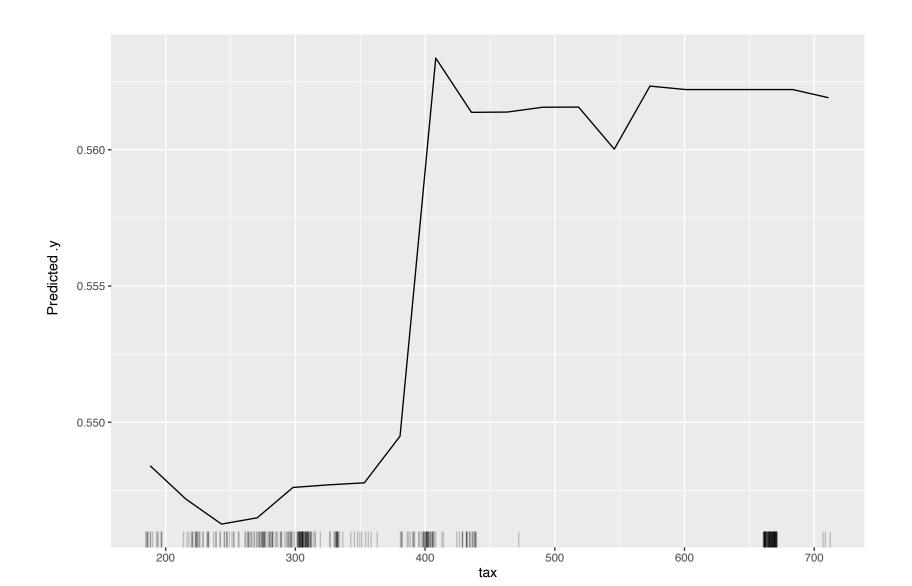
Use the model to generate predictions for this simulated data.

dis	ptratio	$\operatorname{med}\mathbf{v}$	indus	age	tax	rad	Actual Y	Pred Y	dis mean	ptratio	medv	indus	age	tax	rad	Actual Y	Pred Y	mean
3	12.1	13	22.6	90	200	4.3	0.469	0.426	0.488	12.1	13	22.6	90	204	4.3	0.469	0.510	0.516
5	17.2	41	9.1	71	200	2.5	0.538	0.532		17.2	41	9.1	71	204	2.5	0.538	0.532	0.010
6	20.1	31	15.2	88	200	5.1	0.458	0.445	6	20.1	31	15.2	88	204	5.1	0.458	0.495	
2	15	22	5.2	45	200	6.3	0.556	0.550	2	15	22	5.2	45	204	6.3	0.556	0.532	
									المستخدد (مستنسخ								dell'es are a dell'es	
dis	ptratio	$\mathrm{med}\mathbf{v}$	indus	age	tax	$_{ m rad}$	Actual Y	Pred Y	dis mean	ptratio	medv	indus	age	tax	$_{ m rad}$	Actual Y	Pred Y	mean
3	12.1	13	22.6	90	201	4.3	0.469	0.436	2	12.1	13	22.6	90	205	4.3	0.469	0.476	0.501
5	17.2	41	9.1	71	201	2.5	0.538	0.542	0.489	17.2	41	9.1	71	205	2.5	0.538	0.532	0.521
6	20.1	31	15.2	88	201	5.1	0.458	0.445	6	20.1	31	15.2	88	205	5.1	0.458	0.485	
2	15	22	5.2	45	201	6.3	0.556	0.523	2	15	22	5.2	45	205	6.3	0.556	0.561	
							9	المستحسلامست		S						4	المراجع المساحة	- Carrier Maria
								-		,							And in case of the last	and the same of the same
dis	ptratio	$\operatorname{med}\mathbf{v}$	indus	age	tax	rad	Actual Y	Pred Y	dis mean	ptratio	medv	indus	age	tax	rad	Actual Y	Pred Y	mean
dis	ptratio	medv	indus 22.6	age	tax	rad 4.3			dis mean	ptratio 12.1	medv	indus 22.6	age	tax 206	rad 4.3			
	•						Y	Y	mean 0.512	_						Y	Y	mean 0.541
3	12.1	13	22.6	90	202	4.3	Y 0.469	Y 0.526	2	12.1	13	22.6	90	206	4.3	Y 0.469	Y 0.499	
3 5	12.1 17.2	13 41	22.6 9.1	90 71	202 202	4.3 2.5	0.469 0.538	Y 0.526 0.532	$0.51\overset{\scriptscriptstyle 3}{\cancel{2}}$	12.1 17.2	13 41	22.6 9.1	90 71	206 206	4.3 2.5	Y 0.469 0.538	Y 0.499 0.532	
3 5 6	12.1 17.2 20.1	13 41 31	22.6 9.1 15.2	90 71 88	202 202 202	4.3 2.5 5.1	Y 0.469 0.538 0.458 0.556	Y 0.526 0.532 0.475 0.561	$0.51\overset{\scriptscriptstyle 3}{\cancel{2}}$	12.1 17.2 20.1	13 41 31	22.6 9.1 15.2	90 71 88	206 206 206	4.3 2.5 5.1	Y 0.469 0.538 0.458 0.556	Y 0.499 0.532 0.495 0.532	
3 5 6	12.1 17.2 20.1	13 41 31	22.6 9.1 15.2	90 71 88	202 202 202	4.3 2.5 5.1	Y 0.469 0.538 0.458	Y 0.526 0.532 0.475	$\begin{array}{c} 0.51\overset{3}{2}\\ & \overset{6}{2} \end{array}$	12.1 17.2 20.1	13 41 31	22.6 9.1 15.2	90 71 88	206 206 206	4.3 2.5 5.1	Y 0.469 0.538 0.458	Y 0.499 0.532 0.495	0.541
3 5 6 2	12.1 17.2 20.1 15	13 41 31 22	22.6 9.1 15.2 5.2	90 71 88 45	202 202 202 202 202	4.3 2.5 5.1 6.3	Y 0.469 0.538 0.458 0.556	Y 0.526 0.532 0.475 0.561	$\begin{array}{c} 0.512 \\ \begin{array}{c} 6 \\ 2 \end{array}$	12.1 17.2 20.1 15	13 41 31 22	22.6 9.1 15.2 5.2	90 71 88 45	206 206 206 206 206	4.3 2.5 5.1 6.3	Y 0.469 0.538 0.458 0.556	Y 0.499 0.532 0.495 0.532 Pred	0.541 mean
3 5 6 2	12.1 17.2 20.1 15	13 41 31 22 medv	22.6 9.1 15.2 5.2 indus	90 71 88 45	202 202 202 202 202 tax	4.3 2.5 5.1 6.3	Y 0.469 0.538 0.458 0.556 Actual Y	Y 0.526 0.532 0.475 0.561 Pred Y	$\begin{array}{c} 0.51\overset{3}{2}\\ & \overset{6}{2} \end{array}$	12.1 17.2 20.1 15	13 41 31 22 medv	22.6 9.1 15.2 5.2 indus	90 71 88 45	206 206 206 206 206	4.3 2.5 5.1 6.3	Y 0.469 0.538 0.458 0.556 Actual Y	Y 0.499 0.532 0.495 0.532 Pred Y	0.541
3 5 6 2 dis	12.1 17.2 20.1 15 ptratio	13 41 31 22 medv	22.6 9.1 15.2 5.2 indus	90 71 88 45 age	202 202 202 202 202 tax	4.3 2.5 5.1 6.3 rad	Y 0.469 0.538 0.458 0.556 Actual Y 0.469	Y 0.526 0.532 0.475 0.561 Pred Y 0.426	$\begin{array}{c} 0.512 \\ \begin{array}{c} 6 \\ 2 \end{array}$	12.1 17.2 20.1 15 ptratio	13 41 31 22 medv	22.6 9.1 15.2 5.2 indus	90 71 88 45 age	206 206 206 206 206 207	4.3 2.5 5.1 6.3 rad	0.469 0.538 0.458 0.556 Actual Y	Y 0.499 0.532 0.495 0.532 Pred Y 0.426	0.541 mean

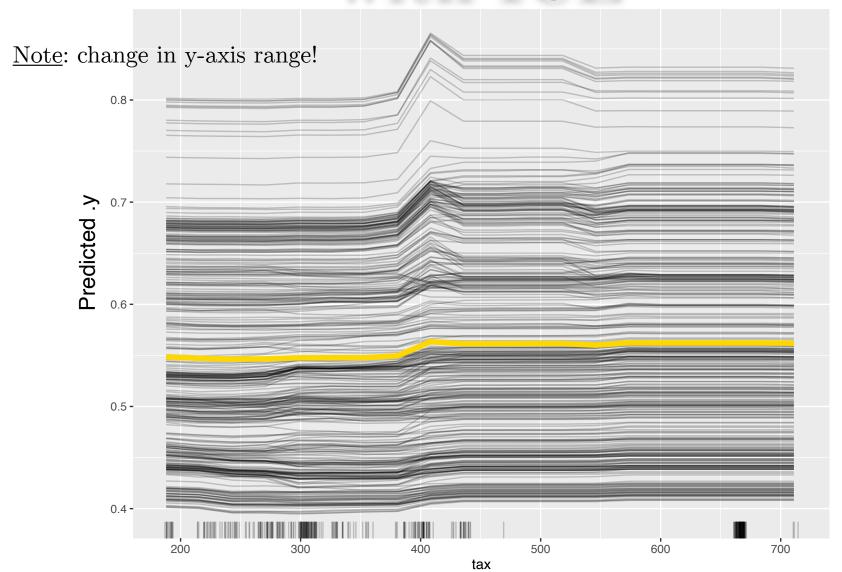
Average the predictions for each replicated dataset (i.e. for each possible value of the variable of interest.)

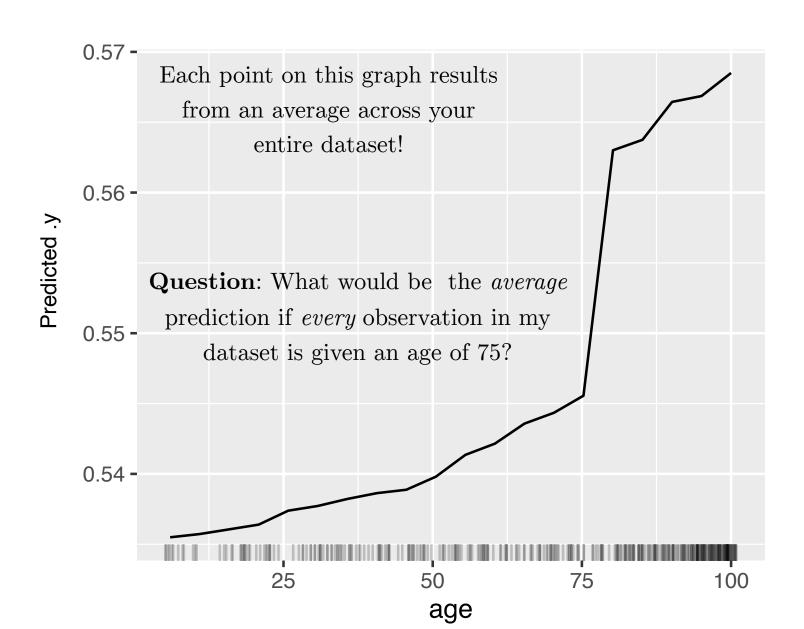
dis	ptratio	medv	indus	age	ax tax	rad	Actual Y	$egin{array}{c} \mathbf{Pred} \ \mathbf{Y} \end{array}$	dis mean	ptratio	medv	indus	age	ax tax	rad	Actual Y	Pred Y	mean
3	12.1	13	22.6	90	200	4.3	0.469	0.426	0.488	12.1	13	22.6	90	204	4.3	0.469	0.510	0.516
5	17.2	41	9.1	71	400	2.5	0.538	0.532		17.2	41	9.1	71		2.5	0.538	0.532	0.010
6	20.1	31	15.2	88	200	5.1	0.458	0.445	6	20.1	31	15.2	88	204	5.1	0.458	0.495	
2	15	22	5.2	45	200	6.3	0.556	0.550	2	15	22	5.2	45	204	6.3	0.556	0.532	Section Control of the
						8		,	San									And are a con-and-are law.
dis	ptratio	medv	indus	age	tax tax	rad	Actual Y	Pred Y	dis mean	ptratio	medv	indus	age	tax tax	rad	Actual Y	Pred Y	mean
3	12.1	13	22.6	90	201	4.3	0.469	0.436	3	12.1	13	22.6	90		4.3	0.469	0.476	
5	17.2	41	9.1	71	201	2.5	0.538	0.542	0.489	17.2	41	9.1	71	205	2.5	0.538	0.532	0.521
6	20.1	31	15.2	88	201	5.1	0.458	0.445	6	20.1	31	15.2	88	205	5.1	0.458	0.485	
2	15	22	5.2	45	201	6.3	0.556	0.523	2	15	22	5.2	45	205	6.3	0.556	0.561	
						<u> </u>)		2		**	
dis	ptratio	medv	indus	age	ax tax	$_{ m rad}$	Actual Y	$egin{array}{c} \operatorname{Pred} \ Y \end{array}$	dis mean	ptratio	medv	indus	age	tax tax	rad	Actual Y	$rac{ ext{Pred}}{ ext{Y}}$	mean
3	12.1	13	22.6	90		4.3	0.469	0.526	3	12.1	13	22.6	90		4.3	0.469	0.499	0 5 4 1
5	17.2	41	9.1	71	202	2.5	0.538	0.532	0.512	17.2	41	9.1	71	206	2.5	0.538	0.532	0.541
6	20.1	31	15.2	88	202	5.1	0.458	0.475	6	20.1	31	15.2	88	206	5.1	0.458	0.495	
2	15	22	5.2	45	202	6.3	0.556	0.561	2	15	22	5.2	45	206	6.3	0.556	0.532	STATE OF STREET
						<u> </u>		,					,		es.		-	
dis	ptratio	$_{ m medv}$	indus	age	tax	$_{ m rad}$	Actual	Pred	dis	ptratio	$_{ m medv}$	indus	age	tax	rad	Actual	Pred	dinativa dista
CID .	puratio	meav	maas	B	tax	raa	Y	Y	mean	puratio	mouv	maas	ug.	tax	raa	Y	Y	mean
3	12.1	13	22.6	90	203	4.3	0.469	0.426	$0.51\overset{3}{3}$	12.1	13	22.6	90	2077	4.3	0.469	0.426	
5	17.2	41	9.1	71	403	2.5	0.538	0.532	0.979	17.2	41	9.1	71	441	2.5	0.538	0.532	0.551
C	20.1	31	15.2	88	203	5.1	0.458	0.512	6	20.1	31	15.2	88	207	5.1	0.458	0.575	1
6	20.1					0.1	0.100	0.012		20.1	01	10.2		, =0.	C 0.1	0.400	0.010	

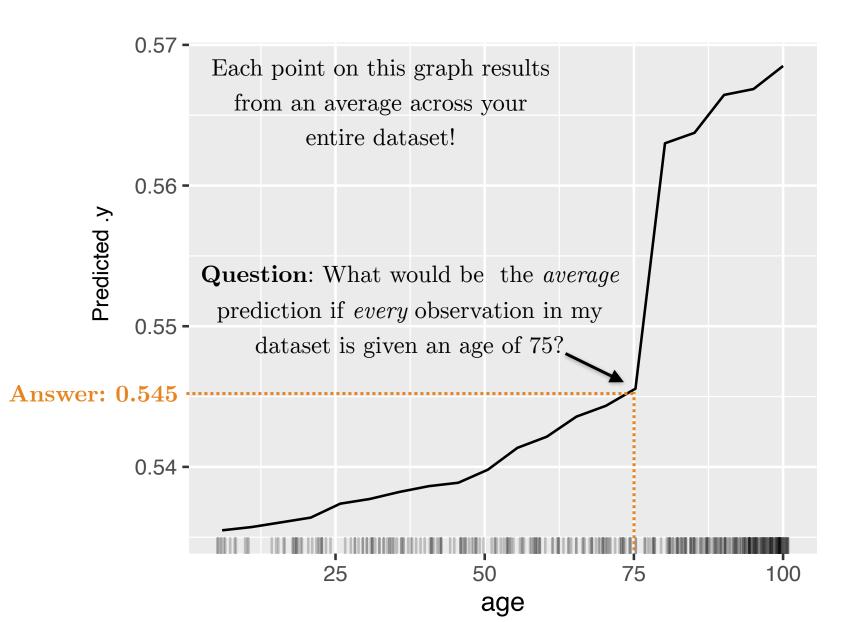
The points on the partial dependence plots are shown in orange

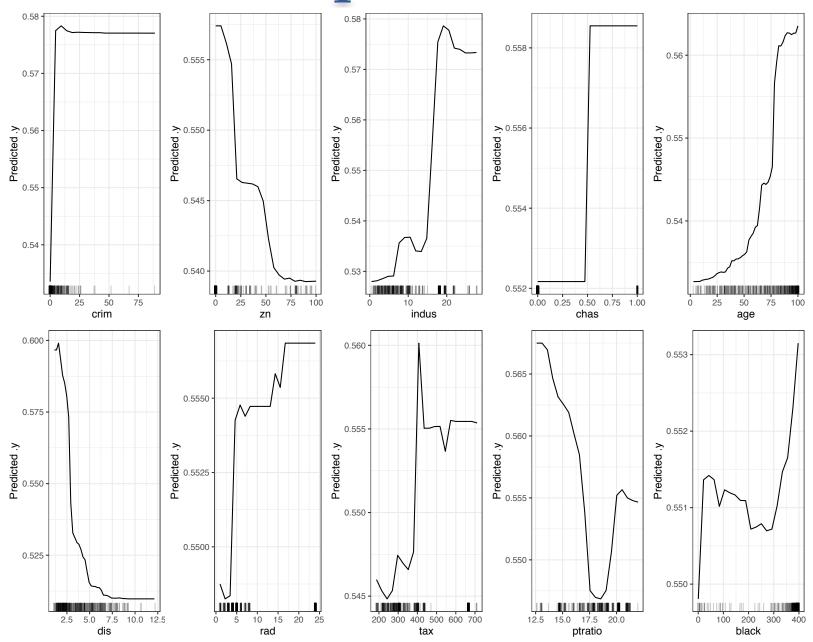


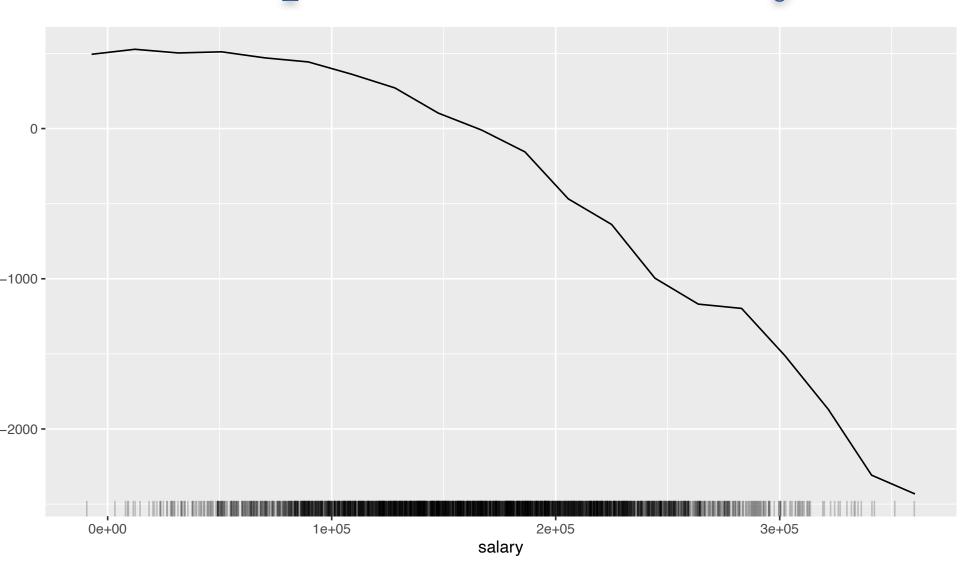
Partial Dependence Plot with ICE

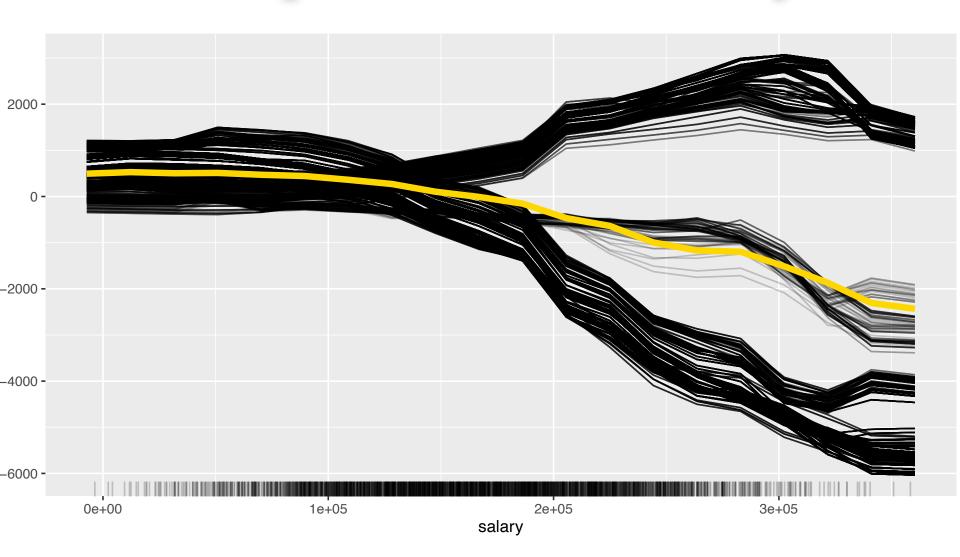


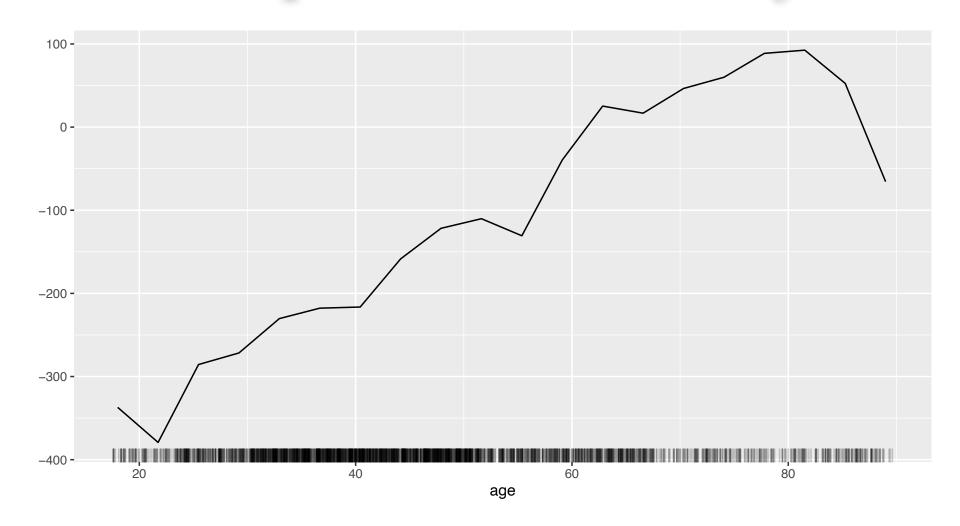


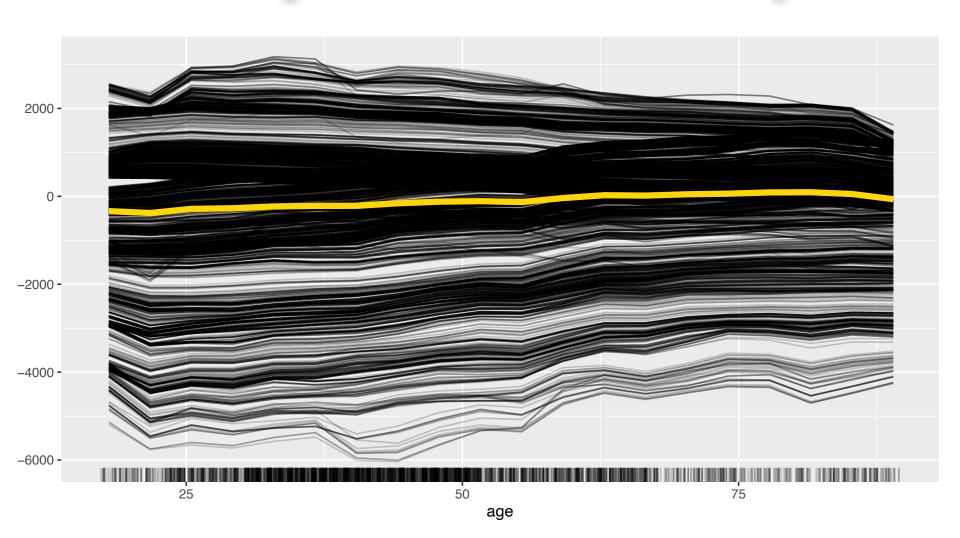












Types of Model Interpretability

	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
$egin{aligned} \mathbf{Model} \\ \mathbf{Agnostic} \end{aligned}$	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

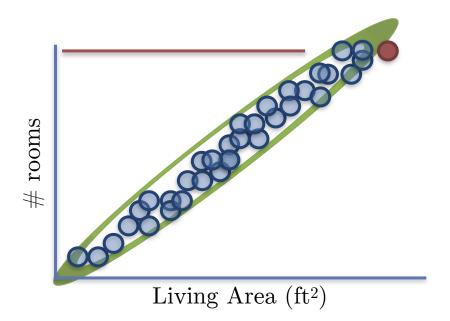
Accumulated Local Effects (ALE)

"Let me show you how the model predictions change when I change the variable of interest to values within a small interval around their current values."

The Primary Problem of Partial Dependence:

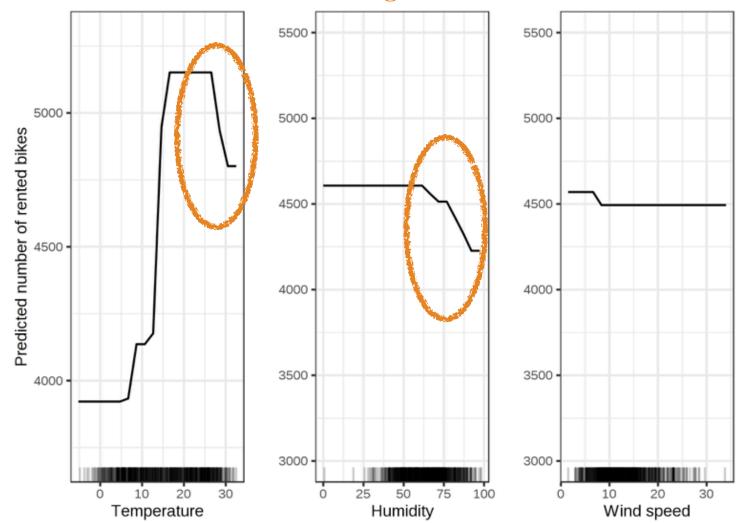
Our visualization (and therefore our conclusions) involve many simulated data points with impossible data values.

Example: A house with 35 rooms will be given all possible values of living area - So we will have <nonsensical> houses with 35 rooms but 500 square feet of area participating in the average value we view on PDP!!



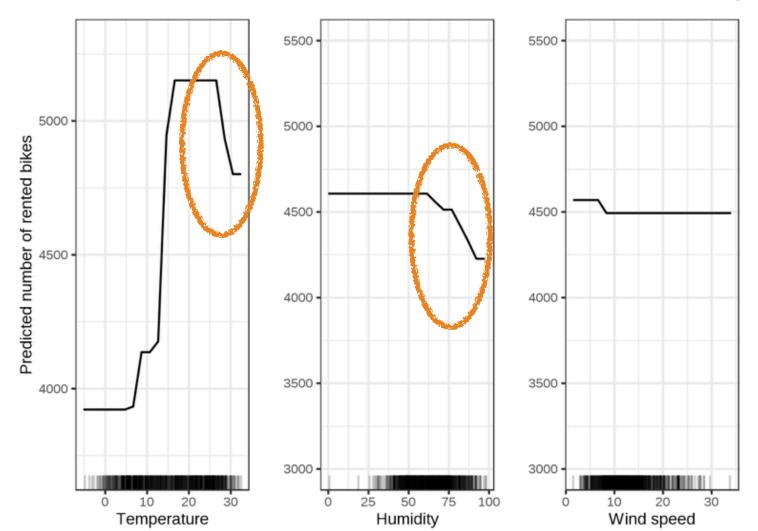
Problem with PDP

As temperature, humidity get too high, bike rentals go down. Makes sense.



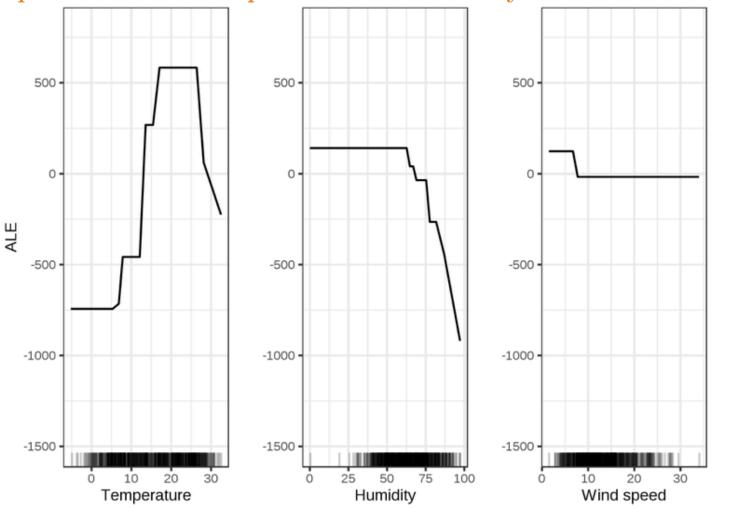
Problem with PDP

BUT, these average predictions involve EVERY observation altered to have high temperature/high humidity - even our observations from November-March! Not trustworthy!



Problem with PDP, Meet Solution with ALE

Using only reasonably contrived data, we get a more clear picture of how temperature and humidity effect bike rentals



Define a Grid

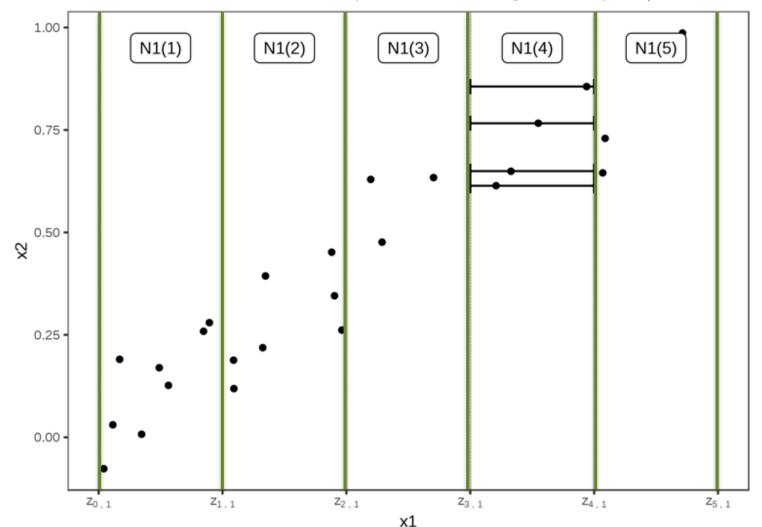
- We left a detail out from our last discussion.
- Remember when we talked about "filling in values across the range of the variable of interest" (ICE slide 25, PDP slide 46)?

dis	ptratio	medv	indus	age	tax	rad	Actual Y	$rac{ ext{Pred}}{ ext{Y}}$
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	
3	12.1	13	22.6	90		4.3	0.469	

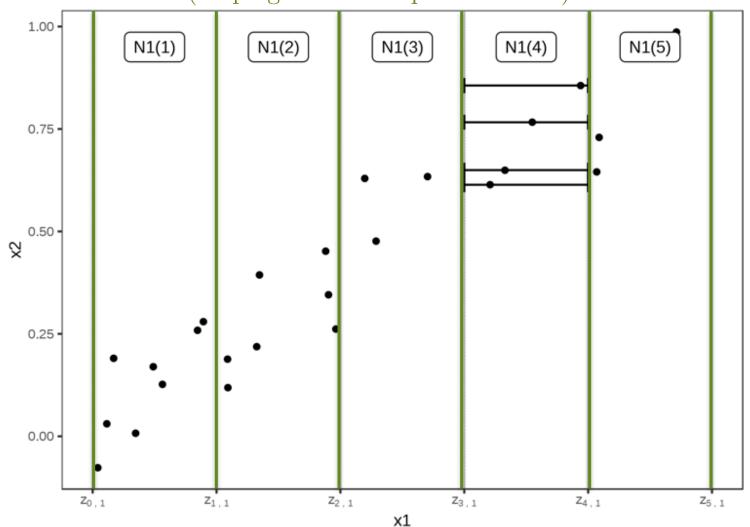
dis	ptratio	medv	indus	age	tax	rad	Actual Y	Pred Y
3	12.1	13	22.6	90	200	4.3	0.469	
3	12.1	13	22.6	90	201	4.3	0.469	
3	12.1	13	22.6	90	202	4.3	0.469	
3	12.1	13	22.6	90	203	4.3	0.469	
3	12.1	13	22.6	90	204	4.3	0.469	
3	12.1	13	22.6	90	205	4.3	0.469	
3	12.1	13	22.6	90	206	4.3	0.469	

- How did I know exactly what values to fill in for tax?
- Well, we have to define this grid before hand. This is generally not a major decision. Equally spaced intervals is common.

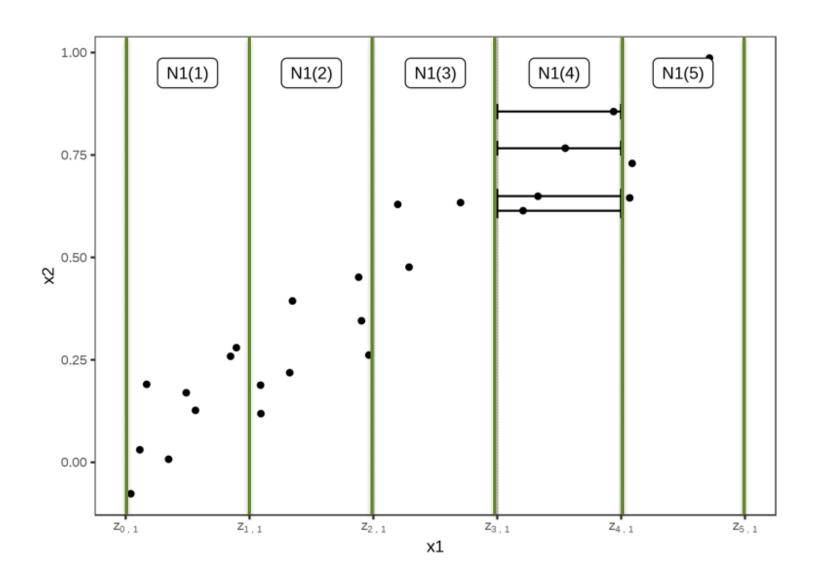
Define a Grid: Most commonly uses quantiles of your data so that the same number of observations fall in each interval. (That gets weird for skewed data because intervals can have very different lengths - try it!)



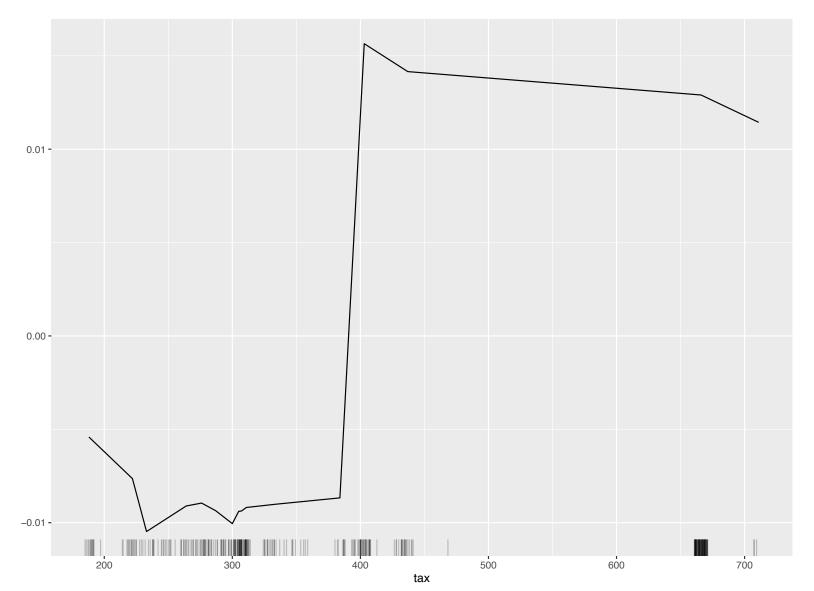
For points in each interval, determine how much their prediction would change if we replace the feature of interest with the upper and lower limits of the interval (keeping all other inputs constant)



These differences are later accumulated and centered, resulting in the ALE curve



These differences are later accumulated and centered, resulting in the ALE curve



Accumulated Local Effects: Some Math

$$\hat{\tilde{f}}_{j,ALE}(x) = \sum_{k=1}^{k_j(x)} \frac{1}{n_j(k)} \sum_{i:x_i^{(i)} \in N_j(k)} \left[f(z_{k,j}, x_{\setminus j}^{(i)}) - f(z_{k-1,j}, x_{\setminus j}^{(i)}) \right]$$

(Uncentered) ALE

Accumulated Local Effects: Some Math

Average over all points in

the interval

$$\hat{\tilde{f}}_{j,ALE}(x) = \sum_{k=1}^{k_j(x)} \frac{1}{n_j(k)} \sum_{i: x^{(i)} \in N:(k)} \left[f(z_{k,j}, x^{(i)}_{\setminus j}) - f(z_{k-1,j}, x^{(i)}_{\setminus j}) \right]$$

All points in the interval (Neighborhood)

Fixing all other variables, for each observation, difference in prediction if variable of interest is set at the upper vs. lower limit of the interval.

(Uncentered) ALE

Accumulated Local Effects: Some Math

ACCUMULATED: The net effect of being in, say the 3rd interval, is the sum of the effects in the 1st, 2nd, 3rd intervals.

$$\hat{\tilde{f}}_{j,ALE}(x) = \sum_{k=1}^{k_j(x)} \frac{1}{n_j(k)} \sum_{i: x_j^{(i)} \in N_j(k)} \left[f(z_{k,j}, x_{\backslash j}^{(i)}) - f(z_{k-1,j}, x_{\backslash j}^{(i)}) \right]$$

LOCAL: Average difference in predictions over points in each interval.

(Uncentered) ALE

ALE after Centering

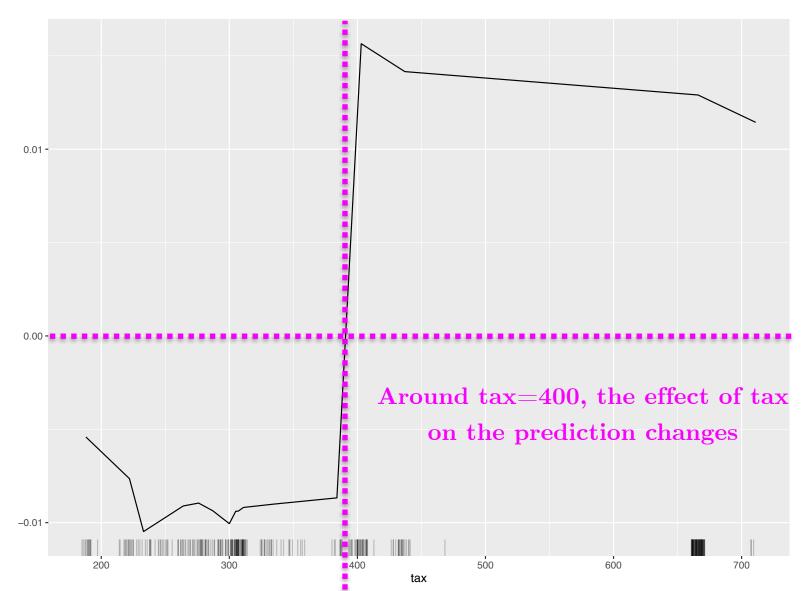
• The final math step is to center the ALE so that the mean effect is zero.

$$\hat{f}_{j,ALE}(x) = \hat{\tilde{f}}_{j,ALE}(x) - \frac{1}{n} \sum_{i=1}^{n} \hat{\tilde{f}}_{j,ALE}(x_j^{(i)})$$

This final value of ALE describes the main effect of the input variable compared to the data's average prediction.

Accumulated Local Effects

These differences are later accumulated and centered, resulting in the ALE curve



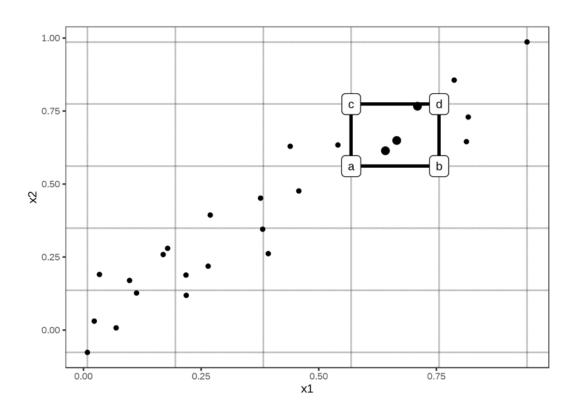
ALE Interpretation

The final value of ALE describes the main effect of the input variable compared to the data's average prediction.

Example: if the ALE for tax is 0.01 when tax=400, this means that when tax=400, the prediction is higher by 0.01 compared to the average prediction.

Second-Order ALE

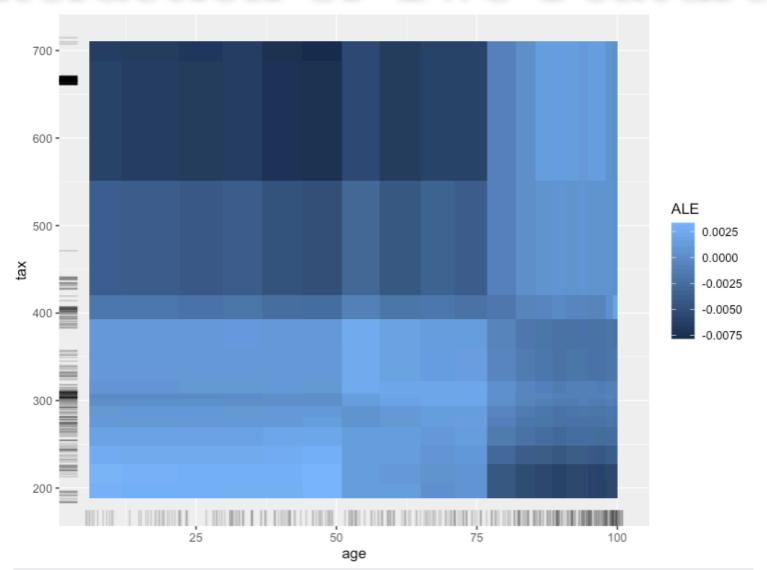
• We can do the same procedure for two input variables simultaneously, defining a rectangular grid to accumulate effects across the 2 dimensions.



ALE plots for the Interaction of Two Features

- We can do the same procedure for two input variables simultaneously, defining a rectangular grid to accumulate effects across the 2 dimensions.
- HOWEVER. This shows us only the second-order interaction effect (a*b) of the two variables, after the main effects have been accounted for.
- Example: $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_1 x_2$ If the interaction term is not really significant, the 2-d ALE plot for the pair (x_1, x_2) would be constant at 0 because the main effects were already accounted for.

ALE plots for the Interaction of Two Features

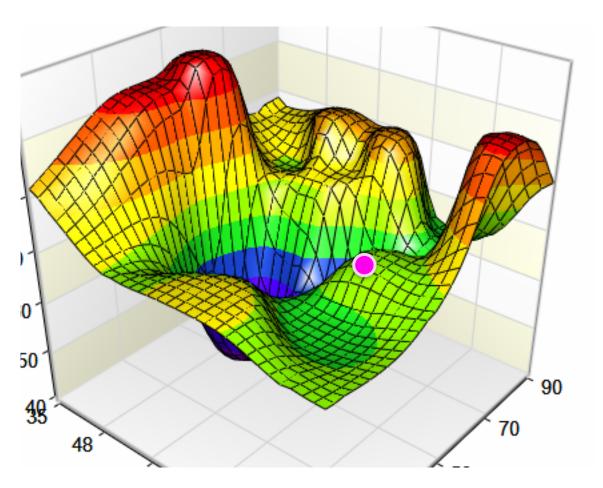


Types of Model Interpretability

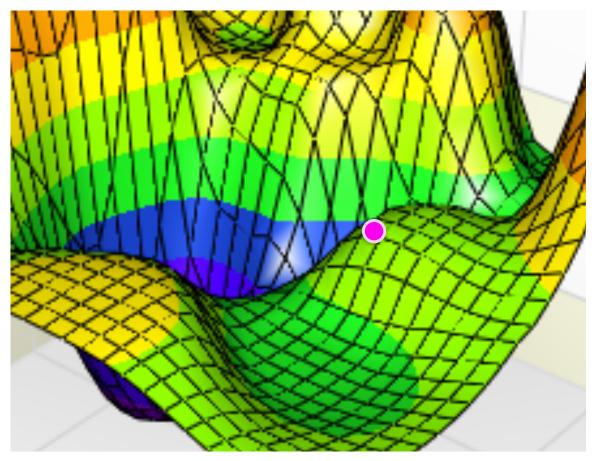
	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
$egin{aligned} \mathbf{Model} \\ \mathbf{Agnostic} \end{aligned}$	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

LIME

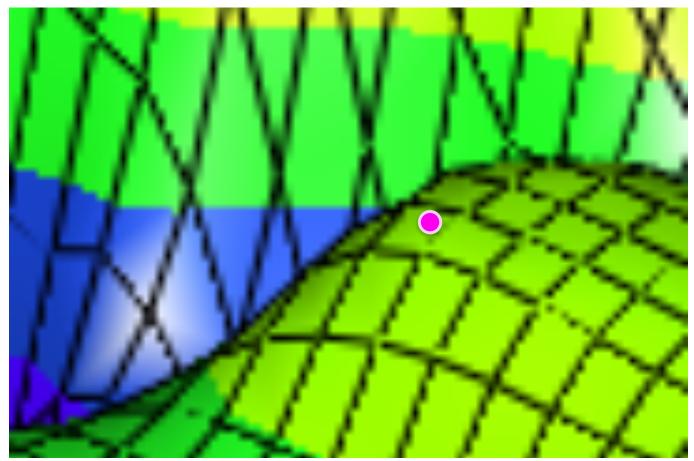
Local Interpretable Model-agnostic Explanations



Zoom in....

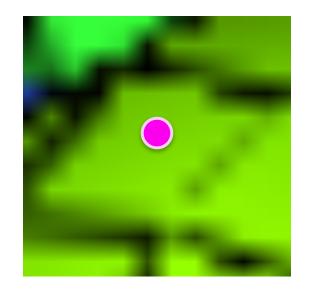


Zoom in....closer



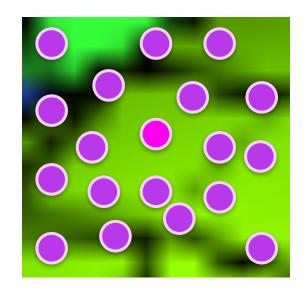
Zoom in....closer

Zoom in....

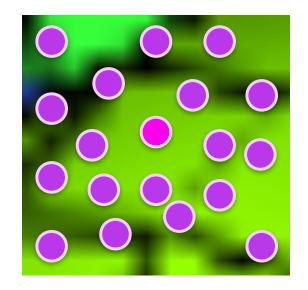


...closer

Just a dot on a flat surface!
We can model that with linear regression!



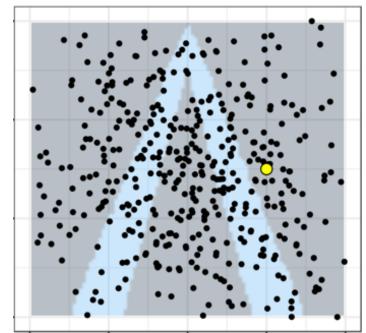
Put a bunch more data points on the function near this pink point of interest, then create a linear model using the purple and pink points as input data.

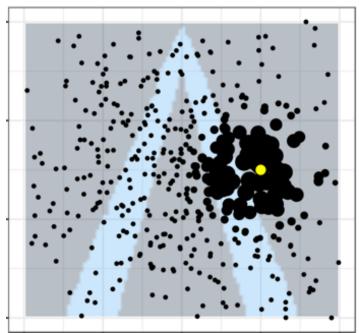


The resulting linear model could explain the exact orientation of the predictive model at the pink point.

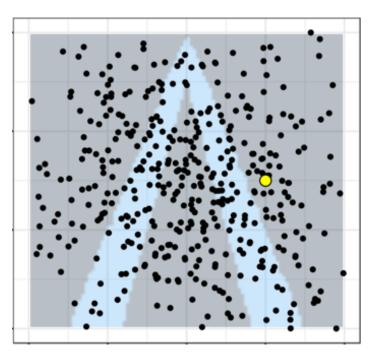
LIME: Details

- LIME doesn't completely ignore the rest of the input space as we showed with the purple dots.
- The points it generates are normally distributed around the data's mean.
- Then the local model weights observations by proximity to the point of interest.

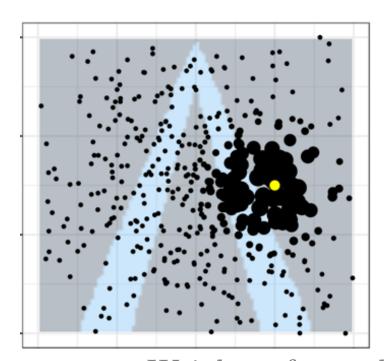




LIME: Details



Normally distributed points sampled across the input domain



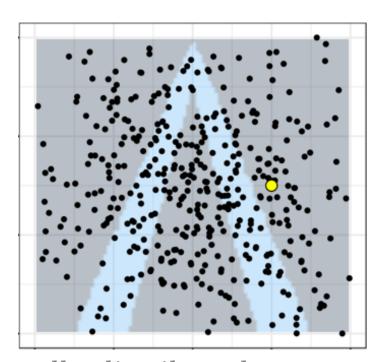
Weights of samples for OLS determined by proximity to yellow point. (i.e. weighted least squares)

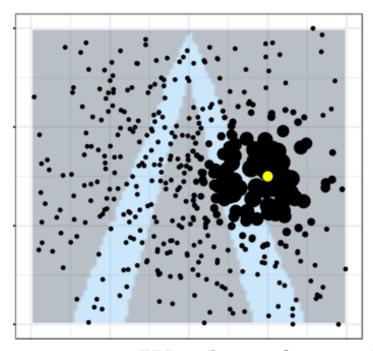
Weighted Least Squares

Weighted least squares gives higher weight to certain observations' residuals in the objective function of OLS.

Observations with higher weight will be more important for the linear model to predict accurately, while the model will not put much emphasis on observations with lower weight.

LIME: Details





Normally distributed points sampled across the input domain

As measured by a Kernel!

Gaussian Radial Basis Function Common

Weights of samples for OLS determined by **proximity** to yellow point.

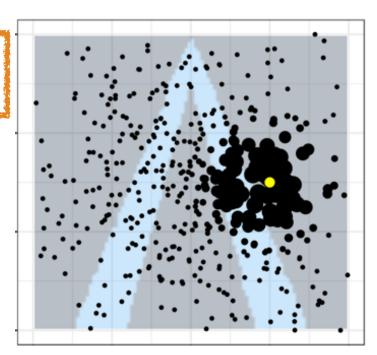
i.e. weighted least squares)

As measured by a Kernel!

Gaussian Radial Basis Function Common

$$e^{\frac{-\|x_i-x\|_2}{2\sigma^2}}$$

How do we determine the width of our kernel, σ ?



Weights of samples for OLS determined by proximity to yellow point.

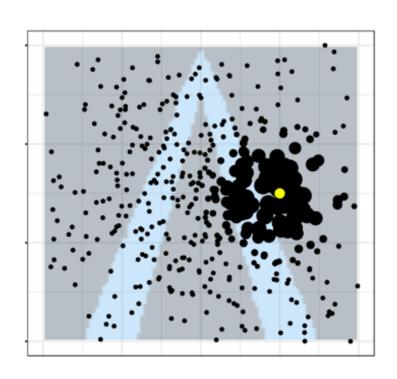
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How do we determine the width of our kernel, σ ?

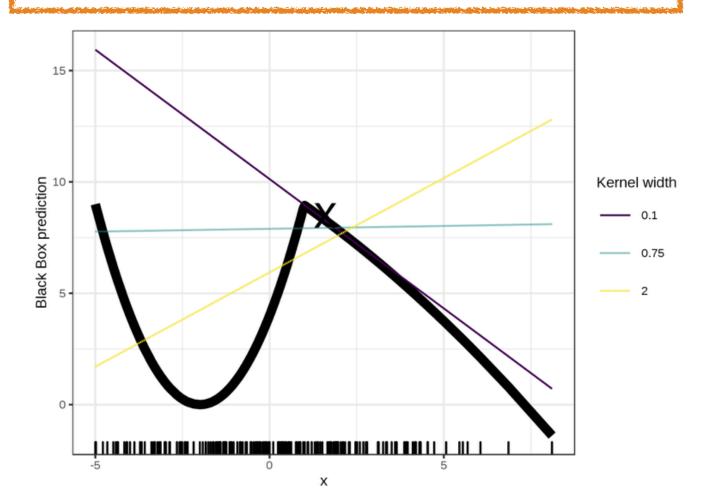


In <u>lime/lime tabular.py</u> you'll get some random default:

if kernel_width is None:
 kernel_width = np.sqrt(training_data.shape[1]) * .75
kernel_width = float(kernel_width)



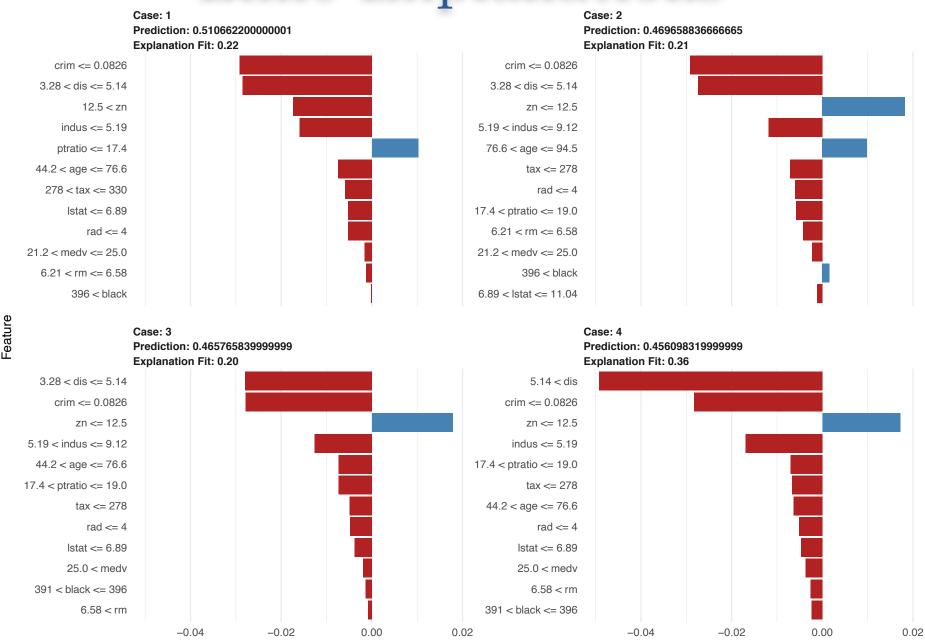
And yes, it matters. Using the wrong kernel width for the wrong point can drastically alter your interpretations



- You have flexibility to choose any interpretable model at the local level
 - Decision trees
 - Lasso
 - OLS w/ stepwise selection
- You have to determine how much explanation you want: decide how complex you want the model to be!
 - Specify lambda
 - Specify sigma in kernel
 - Specify number of variables to use in model
- LIME **commonly used for short** (few variables in local model) **explanations** and **text data**
- Uncommon in compliance scenarios where a *full* explanation is required.

- The correct definition of a "neighborhood" is a **very big**, **unsolved problem** when using LIME with tabular data.
- My recommendation? Only use LIME with text data where the simulated data is created differently:
 - From the document of interest, new documents generated by randomly removing words from original text.
 - Generated data is binary (1 if word is in document, 0 otherwise)
- Data points for local model are sampled from normal distribution, ignoring correlation between features => Unlikely or impossible generated points contribute to conclusions
- If you repeat the sampling procedure, explanations can come out different. Instability => Untrustworthy.

Lime Explanations



Weight

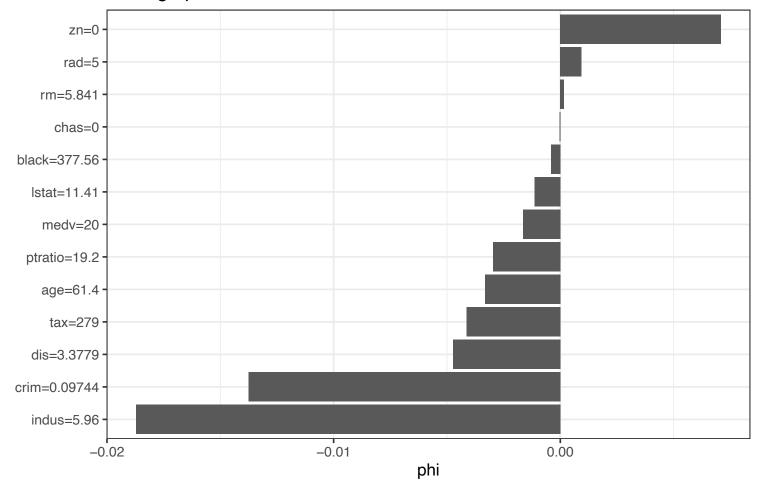
Types of Model Interpretability

	Local	Global
Model Specific	Saliency Maps TreeSHAP	Tree Variable Importance
$egin{aligned} \mathbf{Model} \\ \mathbf{Agnostic} \end{aligned}$	ICE LIME Shapley Values	Permutation Importance Partial Dependence ALE

Interpretation: The value of the j^{th} feature contributed ϕ_j to the prediction of this particular instance compared to the average prediction for the dataset.

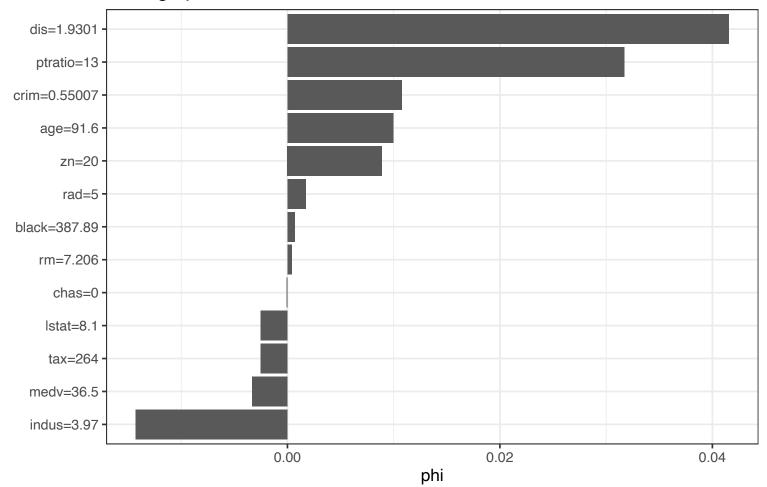
Interpretation: The value of the j^{th} feature contributed ϕ_j to the prediction of this particular instance compared to the average prediction for the dataset.

Actual prediction: 0.50 Average prediction: 0.56



Interpretation: The value of the j^{th} feature contributed ϕ_j to the prediction of this particular instance compared to the average prediction for the dataset.

Actual prediction: 0.64 Average prediction: 0.56



Interpretation: The value of the j^{th} feature contributed ϕ_j to the prediction of this particular instance compared to the average prediction for the dataset.

Best Part: Shapley Values for a given instance sum to the difference between the given prediction and the average prediction.

- Exact definition of Shapley Values is complicated and infeasible to solve for many variables
- Many feasible approximation techniques (more every day) to estimate them.
- Ideas are all similar in spirit to previous methods Monte Carlo simulations to estimate how model changes with and without this precise feature value.

Explains a prediction as a game played by the features, each contributing a portion of points to an overall sum that yields the difference between the prediction of interest and the average prediction.

(variable of interest)

tax chas indus

ptratio zn

rm

black medv

age dis

crime



Explains a prediction as a game played by the features, each contributing a portion of points to an overall sum that yields the difference between the prediction of interest and the average prediction.

```
Observation of Interest:
```

crim zn indus chas nox rm age dis rad tax ptratio black lstat medv $0.55007\ 20\ 3.97$ $0\ 0.647\ 7.206\ 91.6\ 1.9301$ $5\ 264$ $13\ 387.89$ $8.1\ 36.5$

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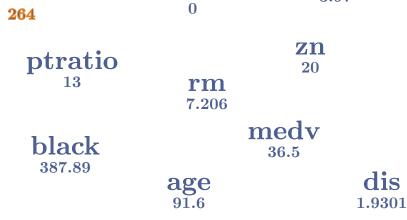
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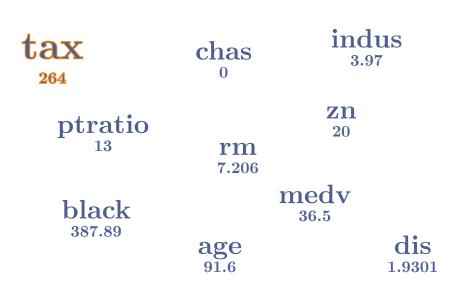
chas

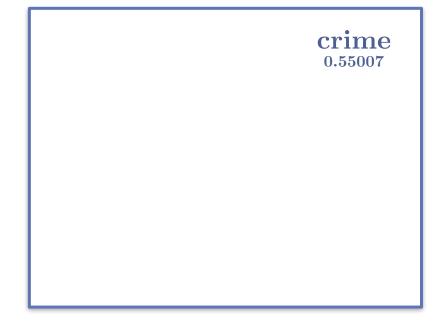
indus
3.97
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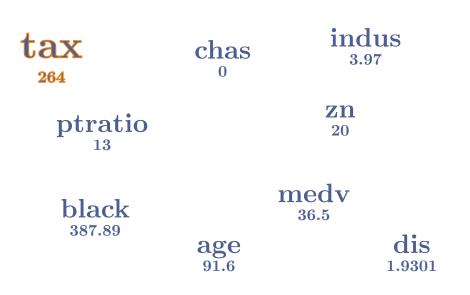


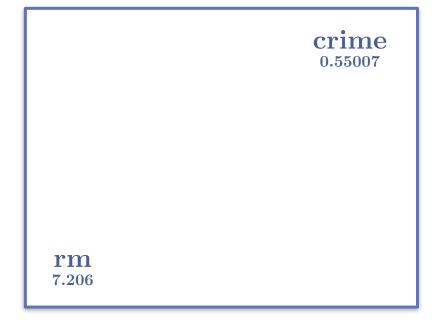
crime 0.55007

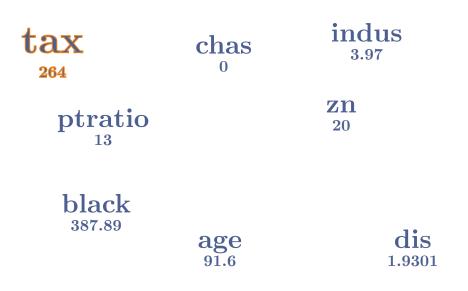
Game play: Features enter a room (black box model) in a random order. All features in the room make contribution to the prediction. The Shapley value of a given feature value is the average change in the prediction that the "coalition" of features already in the room experiences upon being joined by that specific feature value

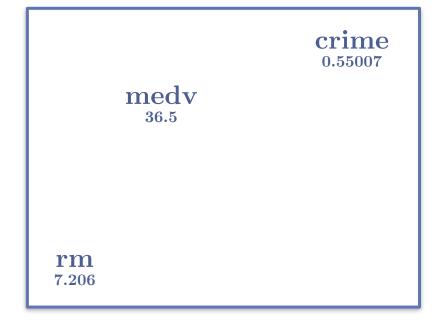


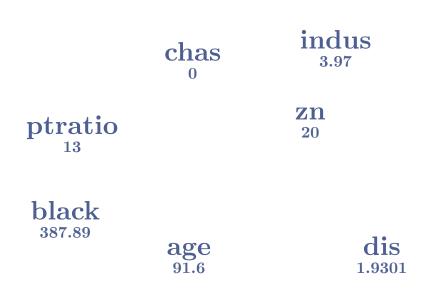


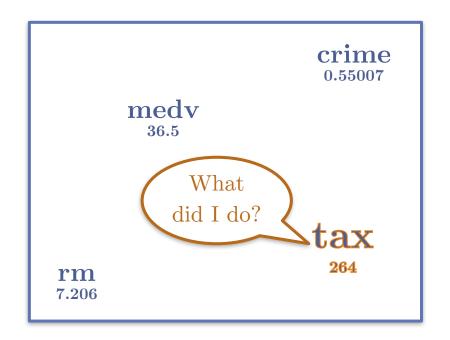




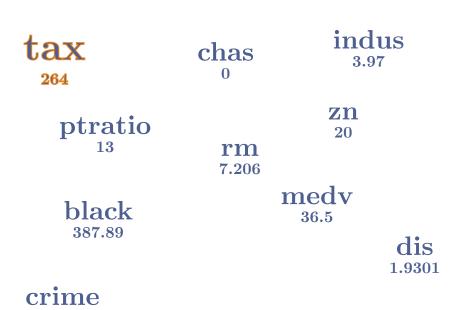








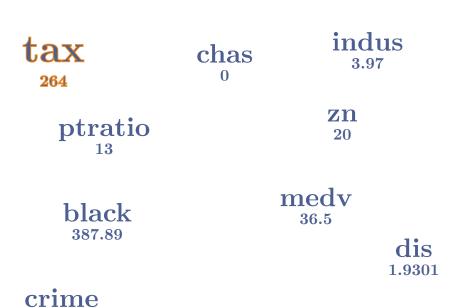
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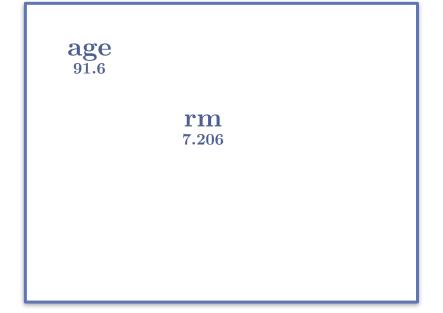
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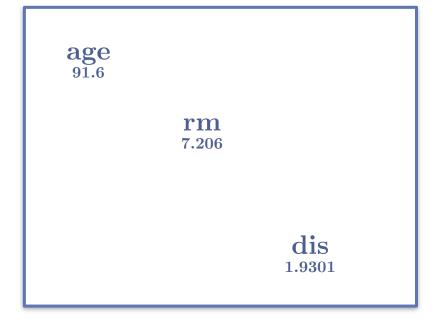
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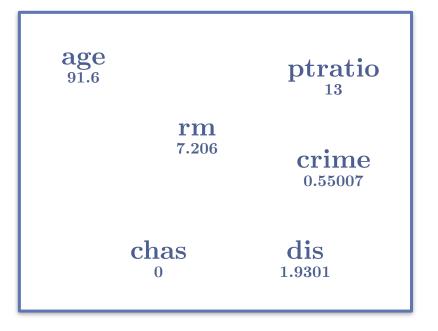
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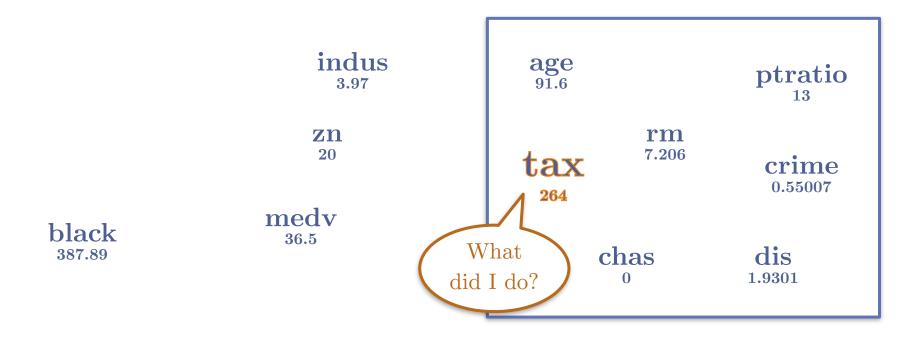
tax 264	$\mathop{\mathrm{chas}}_{\scriptscriptstyle{0}}$	$rac{ ext{indus}}{ ext{3.97}}$
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black 387.89		$\displaystyle \mathop{ m medv}_{_{36.5}}$

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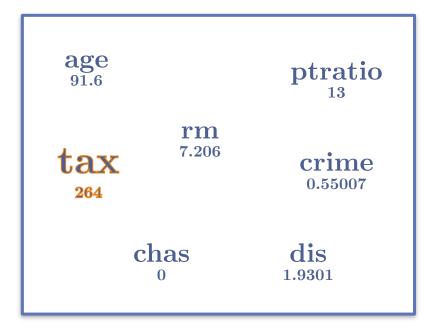
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Features outside of the "room" take on values from a random observation rather than the observation of interest. => explanations built on "Frankenstein" observations

 $\underset{3.97}{\operatorname{indus}}$

zn 20

black 387.89 $\displaystyle \mathop{\mathrm{medv}}_{\scriptscriptstyle{36.5}}$

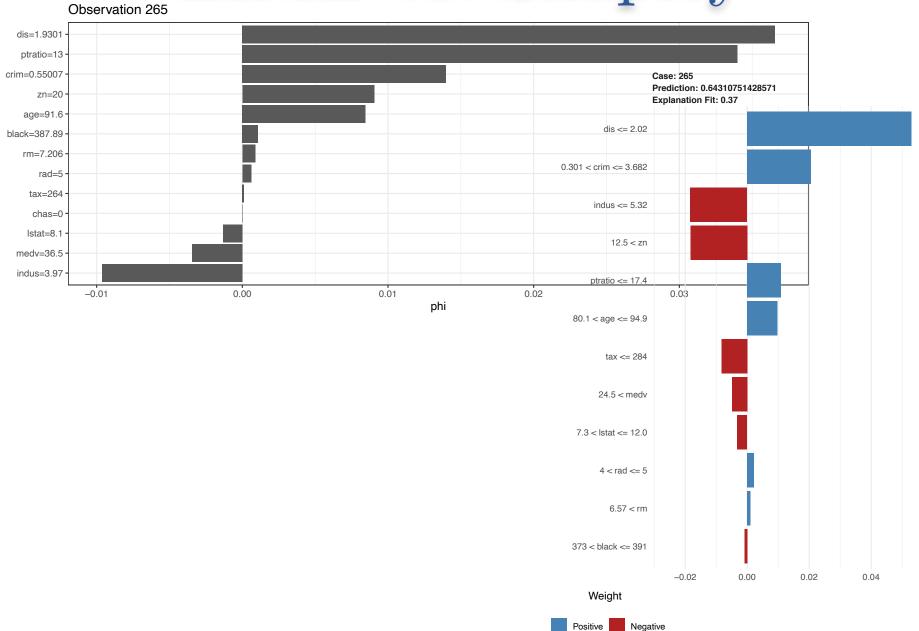


Approximation of Shapley Values

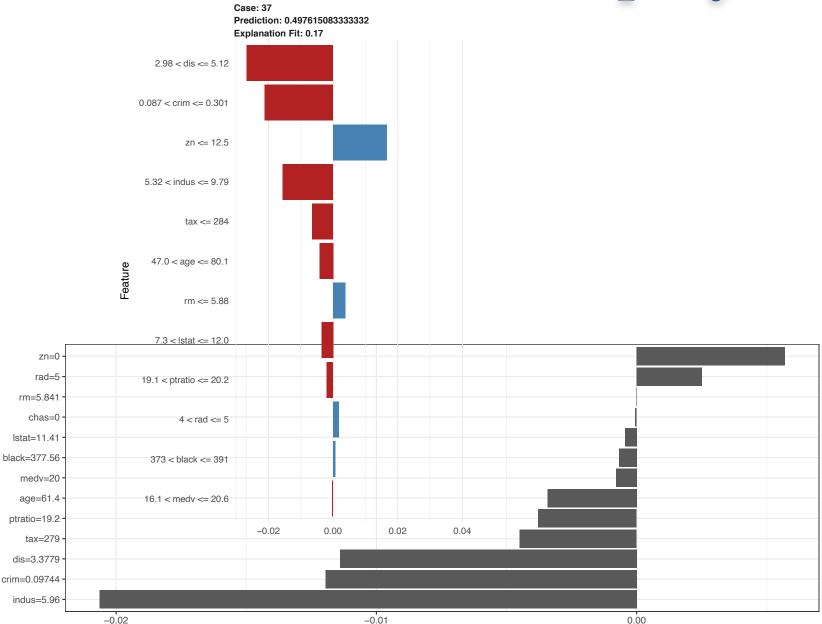
Approximate Shapley estimation for single feature value:

- Output: Shapley value for the value of the j-th feature
- Required: Number of iterations M, instance of interest x, feature index j, data matrix X, and machine learning model f
- For all m = 1,...,M:
 - Draw random instance z from the data matrix X
 - Choose a random permutation o of the feature values
 - \circ Order instance x: $x_o = (x_{(1)}, \ldots, x_{(j)}, \ldots, x_{(p)})$
 - \circ Order instance z: $z_o = (z_{(1)}, \ldots, z_{(j)}, \ldots, z_{(p)})$
 - Construct two new instances
 - lacksquare With feature j: $x_{+j}=(x_{(1)},\ldots,x_{(j-1)},x_{(j)},z_{(j+1)},\ldots,z_{(p)})$
 - \blacksquare Without feature j: $x_{-j} = (x_{(1)}, \ldots, x_{(j-1)}, z_{(j)}, z_{(j+1)}, \ldots, z_{(p)})$
 - \circ Compute marginal contribution: $\phi_{i}^{m}=\hat{f}\left(x_{+j}
 ight)-\hat{f}\left(x_{-j}
 ight)$
- ullet Compute Shapley value as the average: $\phi_j(x) = rac{1}{M} \sum_{m=1}^M \phi_j^m$

LIME vs. Shapley



LIME vs. Shapley



phi

Shapley Values

The Shapley value is the *only* current explanation method with a solid theory, proposed in 4 axioms.

- Efficiency: Feature contributions must add up to the difference of prediction for point of interest vs. the average
- Symmetry: Contributions of two features j and k should be the same if they contribute equally to all possible coalitions
- Dummy: A feature that does not change the predicted value, for any of the coalitions, should have a Shapley value of 0.
- Additivity: For a forest of trees, the Shapley value of the forest for a given point should be the average of the Shapley Values for each tree and that given point.